4.7 Newton's Method

Chapter 4. Applications of Derivatives

4.7 Newton's Method

Note. In Newton's Method, we try to approximate an *x*-intercept of a graph. We use tangent lines to improve our approximations as follows:

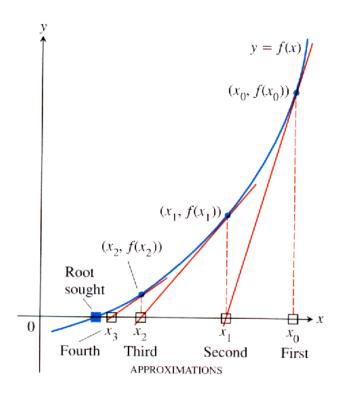


Figure 4.44, page 275

4.7 Newton's Method

Note. Procedure for Newton's Method

- **1.** Guess a first approximation to a solution of the equation f(x) = 0.
- 2. Use the first approximation to get a second, the second to get a third, and so on, using the formula

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}.$$

Note. The equation of the tangent line to y = f(x) at $(x_n, f(x_n))$ is $y - f(x_n) = f'(x_n)(x - x_n)$. Therefore the intercept x_{n+1} satisfies

$$0 - f(x_n) = f'(x_n)(x_{n+1} - x_n)$$
or $x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$

(see page 275 for the algebra steps).

4.7 Newton's Method 3

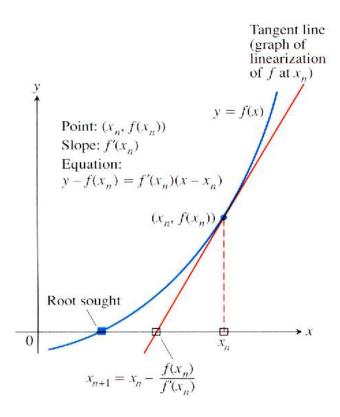


Figure 4.46, page 326 of 11th Edition

Examples. Page 277 number 2, page 278 number 16.