## Chapter 5. Integration5.6 Substitution and Area Between Curves

**Note.** We can use u-substitution in definite integrals:

$$\int_{a}^{b} f(g(x))g'(x)dx = \int_{g(a)}^{g(b)} f(u) \, du$$

where u = g(x), and du = g'(x) dx.

Examples. Page 350 numbers 14a and 18.

**Definition.** If f and g are continuous with  $f(x) \ge g(x)$  throughout [a, b], then the *area* of the region between the curves y = f(x) and y = g(x) from a to b is the integral of [f - g] from a to b:

$$A = \int_a^b [f(x) - g(x)] \, dx.$$



Figure 5.27, Page 347

**Note.** We will take a heuristic shortcut and take "dx" slices.

Examples. Page 351 number 56, Page 352 numbers 66 and 102.