3.9 Related Rates

Chapter 3. Differentiation

3.9 Related Rates

Example. Page 237 number 13.

Note. Related Rates Problem Strategy

We will follow this protocol when solving related rates problems:

- **Step 1.** Draw a picture and name the variables and constants. Use t for time. Assume that all variables are differentiable functions of time.
- **Step 2.** Write down the numerical information (in terms of the symbols you have chosen) and write down what you are asked to find (usually a rate, expressed as a derivative).
- **Step 3.** Write an equation that relates the variables. You may have to combine two or more equations to get a single equation that relates the variable whose rate you want to the variables whose rates you know.

3.9 Related Rates

Step 4. Differentiate with respect to t. Then express the rate you want in terms of the rate and variables whose values you know.

Step 5. Evaluate. Use known values to find the unknown rate.

Example. Page 237 number 13 (again).

Examples. Page 238 number 18, page 239 number 30, and page 240 number 38.