

# Calculus 2, Chapter 8 Study Guide

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The following is a *brief* list of topics covered in Chapter 8 of *Thomas' Calculus*. Test questions will be chosen directly from the text. This list is not meant to be comprehensive, but only gives a list of several important topics. I reserve the right to ask you definitions and theorems on the tests. If I do so, then I will choose from the **bold-faced** items below.

**8.1. Integration by Parts.** Integration by Parts,  $\int e^x \sin x \, dx$  and related methods, reduction formulas.

**8.2. Trigonometric Integrals.**  $\int \sin^m x \cos^n x \, dx$ , integration powers of  $\tan x$  or  $\sec x$ ; using trig identities for  $\int \sin mx \sin nx \, dx$ ,  $\int \sin mx \cos nx \, dx$ , and  $\int \cos mx \cos nx \, dx$ .

**8.3. Trigonometric Substitution.** Integrals involving  $a^2 + x^2$ ,  $a^2 - x^2$ , and  $x^2 - a^2$ ; trig substitution, reference triangles.

**8.4. Integration of Rational Functions by Partial Fractions.** Linear factors, irreducible quadratic factors, factors of higher order (or “multiplicity”), Heaviside Cover-Up Method.

**8.5. Integral Tables and Computer Algebra Systems.** Use of the Table of Integrals on pages T1–T5, using the TI-89, substitution and completing the square to get into standard form.

**8.6. Numerical Integration.** Trapezoid Rule and its error bound, Simpson's Rule and its error bound.

**8.7. Improper Integrals.** Improper integrals of Type I ( $\int_{-\infty}^{\infty} f(x) \, dx$ ), improper integrals of Type II (integrals over vertical asymptotes, for example), convergence and divergence of improper integrals, **Direct Comparison Test**, **Limit Comparison Test**.