## Introduction to Algebra, MATH 4127

Homework 5, Sections II.8 and II.9

Due Friday October 10, 2014 at 2:30

Write in complete sentences!!! *Explain* what you are doing and convince me that you understand what you are doing and why. Justify all steps by quoting the relevant results from the textbook.

**II.8.4.** Consider the permutations in  $S_6$ :

$$\sigma = \left(\begin{array}{rrrrr} 1 & 2 & 3 & 4 & 5 & 6 \\ 3 & 1 & 4 & 5 & 6 & 2 \end{array}\right) \text{ and } \tau = \left(\begin{array}{rrrrr} 1 & 2 & 3 & 4 & 5 & 6 \\ 2 & 4 & 1 & 3 & 6 & 5 \end{array}\right)$$

Calculate  $\sigma^{-2}\tau$ .

- **II.8.46.** Show that  $S_n$  is a nonabelian group for  $n \ge 3$ . HINT: Compose a rotation with a "flip" (in the examples in class, the "flips" were divided into mirror images and diagonal flips). Do this for general n.
- **II.8.A. (Bonus)** Let G be a group of permutations on a set S. Let  $s \in S$  and define  $\operatorname{stab}(s) = \{\alpha \in G \mid \alpha(s) = s\}$ . Then  $\operatorname{stab}(s)$  is the *stabilizer of s in G*. Prove that  $\operatorname{stab}(s)$  is a subgroup of G.
- **II.9.3.** Find all orbits of the permutation

Show your work.

II.9.11 Express

as a product of disjoint cycles and then as a product of transpositions.