

1. Section 1-1

Find the vector with initial point P_1 and final point P_2 . Sketch the result in either the xy -plane or in R^3 , whichever is appropriate.

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| 1. $\overrightarrow{P_1P_2} = \langle 1, 2 \rangle$ | 11. $\mathbf{u} + \mathbf{v} = \langle 3, 8 \rangle$ |
| 3. $\overrightarrow{P_1P_2} = \langle -4, -2, -2 \rangle$ | 13. $\mathbf{u} + \mathbf{v} = \langle -2, 3 \rangle$ |
| 5. $\overrightarrow{P_1P_2} = \langle 1, 10, 4 \rangle$ | 15. $\mathbf{u} + \mathbf{v} = \langle 1, 1, 0 \rangle$ |
| 7. $\overrightarrow{P_1P_2} = \langle -7, 20, 4 \rangle$ | 17. $\mathbf{u} + \mathbf{v} = \langle 2, 4, 5 \rangle$ |
| 9. $\overrightarrow{P_1P_2} = \langle 1, 2, 3 \rangle$ | |

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| 19. $\mathbf{L}(t) = \langle t, 5t + 7 \rangle$ | $\mathbf{K}(s) = \langle s + 1, 5s + 2 \rangle$ |
| 21. $\mathbf{L}(t) = \langle t + 2, 2t + 3 \rangle$ | $\mathbf{K}(s) = \langle s + 3, 2s + 5 \rangle$ |
| 23. $\mathbf{L}(t) = \langle -4t + 7, -2t + 9, -2t + 2 \rangle$ | $\mathbf{K}(s) = \langle -4s + 3, -2s + 7, -2s \rangle$ |
| 25. $\mathbf{L}(t) = \langle t - 4, 20t - 17, 4t + 1 \rangle$ | $\mathbf{K}(s) = \langle s - 3, 20s + 3, 4s + 5 \rangle$ |
| 27. $\mathbf{L}(t) = \langle -te + \pi, t\pi + e, -2t + 2 \rangle$ | $\mathbf{K}(s) = \langle -se + \pi - e, s\pi + \pi + e, -2s \rangle$ |

2. Section 1-2

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| 1. $\ \mathbf{u}\ = 5, \ \mathbf{v}\ = 2, \theta = 36.869^\circ$ | 11. $k = -12$ |
| 3. $\ \mathbf{u}\ = 5.009, \ \mathbf{v}\ = 9.214, \theta = 23.839^\circ$ | 13. $k = 2$ |
| 5. $\ \mathbf{u}\ = 10, \ \mathbf{v}\ = 10, \theta = 90^\circ$ | 15. <i>no solution</i> |
| 7. $\ \mathbf{u}\ = 3, \ \mathbf{v}\ = 6.324, \theta = 42.45^\circ$ | 17. $k = 1.104$ |
| 9. $\ \mathbf{u}\ = 1, \ \mathbf{v}\ = 1, \theta = 90^\circ$ | 19. $k = -1$ or $k = -6$ |
| 21. $\mathbf{p} = \langle 1, 7 \rangle, \mathbf{v} = \langle 2, 11 \rangle$ | $proj_{\mathbf{p}}(\mathbf{v}) = \langle 1.58, 11.06 \rangle$ |
| 23. $\mathbf{p} = \langle 1, 2, 1 \rangle, \mathbf{v} = \langle 2, 2, 7 \rangle$ | $proj_{\mathbf{p}}(\mathbf{v}) = \langle \frac{13}{6}, \frac{13}{3}, \frac{13}{6} \rangle$ |
| 25. $\mathbf{p} = \mathbf{j}, \mathbf{v} = 2\mathbf{i} - 3\mathbf{j} + 4\mathbf{k}$ | $proj_{\mathbf{p}}(\mathbf{v}) = -3\mathbf{j}$ |
| 27. $\mathbf{p} = \mathbf{i} + 2\mathbf{j}, \mathbf{v} = \mathbf{i} + 7\mathbf{j}$ | $proj_{\mathbf{p}}(\mathbf{v}) = 3\mathbf{i} + 6\mathbf{j}$ |

3. Section 1-3

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| 1. $\mathbf{u} \times \mathbf{v} = \langle 0, 0, -1 \rangle$ | 15. $Area = \frac{\sqrt{3}}{2}$ |
| 3. $\mathbf{u} \times \mathbf{v} = \langle 0, 0, -6 \rangle$ | 17. $Area = \frac{3}{2}\sqrt{2}$ |
| 5. $\mathbf{u} \times \mathbf{v} = \langle 0, 0, 1 \rangle$ | 19. $\mathbf{u} \times \mathbf{v} = -2\mathbf{k}$ |
| 7. $\mathbf{u} \times \mathbf{v} = \langle -6, 39, -15 \rangle$ | 21. $\mathbf{u} \times \mathbf{v} = 5\mathbf{i} - \mathbf{j} - 3\mathbf{k}$ |
| 9. $\mathbf{u} \times \mathbf{v} = \langle 0, 0, 0 \rangle$ | 23. $\mathbf{u} \times \mathbf{v} = -b\mathbf{i} + a\mathbf{j}$ |
| 11. $Area = 3/2$ | 25. $\mathbf{u} \times \mathbf{v} = b\mathbf{i} - a\mathbf{k}$ |
| 13. $Area = 2$ | |

4. Section 1-4

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| 1. $Volume = 12$ | 13. $z = 0$ |
| 3. $Volume = 4$ | 15. $y = x$ |
| 5. $Volume = 5$ | 17. $z = 3$ |
| 7. $Volume = lwh$ | 19. $y = \frac{3}{2}x$ |
| 9. $z = \frac{x+y}{3}$ | 21. $z = 0$ |
| 11. $z = -\frac{7}{2}x - \frac{11}{4}y + \frac{55}{4}$ | 23. $z = \frac{1}{2}x + y$ |

5. Section 1-5

Equation only: No sketches.

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| 1. $y = x + 2$ | 17. $x - 1 + \frac{(y-2)^2}{9} = 1$ |
| 3. $y^3 = x^2$ | 19. $3y = 4x^2 - 2$ |
| 5. $y = x - 1 + 2\sqrt{x-1}$ | 21. $(x-1)^2 + y^2 = 1$ |
| 7. $x^2 + y^2 = 4$ | 23. $x + y = 1$ |
| 9. $\frac{x^2}{4} + \frac{y^2}{9} = 1$ | 25. $\mathbf{r}(\theta) = \langle 3 \cos(\theta) + 1, 3 \sin(\theta) + 1 \rangle$ |
| 11. $y = 2x^2 - 1$ | 27. $\mathbf{r}(\theta) = \langle 5 \cos(\theta) + 1, 5 \sin(\theta) - 3 \rangle$ |
| 13. $\frac{(x-1)^2}{4} + y^2 = 1$ | 29. $\mathbf{r}(t) = \langle 3 \cos(5t) + 1, 3 \sin(5t) + 1 \rangle$ |
| 15. $(x-1)^2 + (y-2)^2 = 1$ | |

6. Section 1-6

1. $\mathbf{v}(t) = \langle 2t, 3t^2, 4t^3 \rangle$, $\mathbf{a}(t) = \langle 2, 6t, 12t^2 \rangle$
3. $\mathbf{v}(t) = \left\langle -\frac{1}{t^2}, -\frac{2}{t^3}, -\frac{3}{2t^{5/2}} \right\rangle$, $\mathbf{a}(t) = \left\langle \frac{2}{t^3}, \frac{6}{t^4}, \frac{15}{4t^{7/2}} \right\rangle$
5. $\mathbf{v}(t) = \langle -3 \sin t, 5 \cos t, -4 \sin t \rangle$, $\mathbf{a}(t) = \langle -3 \cos t, -5 \sin t, -4 \cos t \rangle$
7. $\mathbf{v}(t) = \langle [\sec^2 t, -\csc^2 t, \sec(t) - \csc t \cot t] \rangle$, $\mathbf{a}(t) = \langle [2 \tan t \sec^2 t, -2 \cot t \csc^2 t, \csc t \cot^2 t + \sec t] \rangle$
9. $\mathbf{v}(t) = \langle 0, 0, \tan t \rangle$, $\mathbf{a}(t) = \langle 0, 0, \sec^2(t) \rangle$,
11. $\mathbf{v}(t) = \left\langle 2t, \frac{1}{1+t^2} \right\rangle$, $\mathbf{a}(t) = \left\langle 2, -\frac{2t}{(1+t^2)^2} \right\rangle$
13. $\mathbf{v}(t) = \langle -e^{-t} \sin t + e^{-t} \cos t, -e^{-t} \cos t - e^{-t} \sin t, -e^{-t}t + e^{-t} \rangle$, $\mathbf{a}(t) = \langle -2e^{-t} \cos t, 2e^{-t} \sin t, e^{-t} - 1 \rangle$

Velocity only: No sketch.

15. $\mathbf{v}(1) = \langle 2, 4 \rangle$
17. $\mathbf{v}\left(\frac{\pi}{6}\right) = \left\langle -\frac{1}{2}, \frac{1}{2}\sqrt{3} \right\rangle$
19. $\mathbf{v}(0) = \langle 1, -1 \rangle$
21. $\mathbf{v}(2) = \langle 3, 2 \rangle$

23. $\mathbf{r}(t) = \langle t, 2t, 64t - 16t^2 \rangle$
 plane: $y = 2x$
 $t_{\max} = 2$
25. $\mathbf{r}(t) = \langle 1 + 72t, 3 + 38t, 65t - 16t^2 \rangle$
 plane: $\frac{89}{36} + \frac{19}{36}x = y$
 $t_{\max} = 2.03125$
27. $\mathbf{r}(t) = \langle 0, 0, -16t^2 \rangle$
 plane: undefined
 $t_{\max} = 0$
29. $\mathbf{r}(t) = \langle 72t, 38t, 65t - 16t^2 \rangle$
 plane: $72y = -32x$
 $t_{\max} = 2.03125$

7. Section 1-7

1. $\mathbf{T}(t) = \left\langle \frac{3}{5}, \frac{4}{5} \right\rangle, v = 5$
3. $\mathbf{T}(t) = \langle -\sin(2t), \cos(2t) \rangle, v = 2$
5. $\mathbf{T}(t) = \left[\frac{2t^2}{2t^2+1}, \frac{2t}{2t^2+1}, \frac{1}{2t^2+1} \right], v = 2t^2 + 1$
7. $\mathbf{T}(t) = \left\langle \frac{3}{5} \cos(t^2), \frac{4}{5} \cos(t^2), -\sin(t^2) \right\rangle, v = 10t^2$
9. $\mathbf{T}(t) = \left\langle \frac{2e^{2t}}{2e^{2t}+1}, \frac{2e^t}{2e^{2t}+1}, \frac{1}{2e^{2t}+1} \right\rangle, v = 2e^{2t} + 1$
11. $L = 10$
13. $L = 2\pi$
15. $L = 2\pi$
17. $L = 2\pi$
19. $L = 3 + \ln(2)$
21. $L = \frac{20}{27}\sqrt{10} - \frac{2}{27}$
23. $s(t) = t^3$
25. $s(t) = 5t^2$
27. $s(t) = e^{2t} + t - 1$

8. Section 1-8

1. $\mathbf{N} = \left\langle \frac{-4}{5}, \frac{3}{5} \right\rangle, \kappa(t) = 0$
3. $\mathbf{N} = \langle -\cos(2t), -\sin(2t) \rangle, \kappa(t) = 1$
5. $\mathbf{N} = \langle -\cos(t), -\sin(t), 0 \rangle, \kappa(t) = \frac{3}{25}$
7. $\mathbf{r}(t) = \left\langle \frac{2t}{2t^2+1}, \frac{2t^2-1}{2t^2+1}, \frac{-2t}{2t^2+1} \right\rangle, \kappa(t) = \frac{2t}{(2t^2+1)^2}$
9. $\mathbf{r}(t) = \left\langle -\frac{3}{5} \sin(t^2), -\frac{4}{5} \sin(t^2), -\cos(t^2) \right\rangle, \kappa(t) = \frac{1}{5}$
11. $\frac{dv}{dt} = 0, \kappa(t) = 1$
13. $\frac{dv}{dt} = \frac{2t^2-1}{t^2}, \kappa(t) = \frac{2t}{(2t^2+1)^2}$
15. $\frac{dv}{dt} = 2\sqrt{6} \cos 2t, \kappa(t) = 0$
17. $\frac{dv}{dt} = 4e^{2t}, \kappa(t) = \frac{2e^t}{(2e^t+1)^2}$