

PHYS-2010GENERAL PHYSICS IDR. LUTTERMOSER'S CLASSPROBLEM SET I

1.

$$s = \frac{1}{2} a t^2$$

$$[t] = T \text{ (time)}, [a] = LT^{-2} \text{ (length per time squared)}$$

$$[\frac{1}{2}] = 1 \text{ (unitless)}, [s] = L \text{ (length = displacement)}$$

$$[s] = [\frac{1}{2}] [a]^m [t]^n$$

$$L = 1 \cdot (LT^{-2})^m (T)^n$$

$$L = L^m T^{-2m} T^n = L^m T^{n-2m}$$

As such,  $m = 1$  for LHS = RHS in length, then

$$1 = T^{n-2m} = T^{n-2 \cdot 1} = T^{n-2}$$

Since  $T$  does not appear on the LHS,  $n = 2$ , then

$$1 = T^{2-2} = T^0 = 1 \quad \checkmark$$

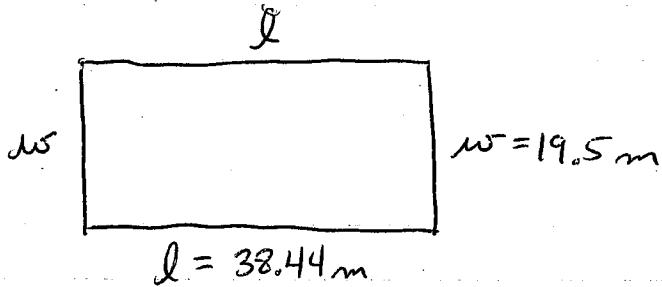
The value for  $\frac{1}{2}$  can then be found with a little algebra:

$$s = \frac{1}{2} a t^2$$

$$\boxed{\frac{1}{2} = \frac{s}{at^2}}$$

(1-2)

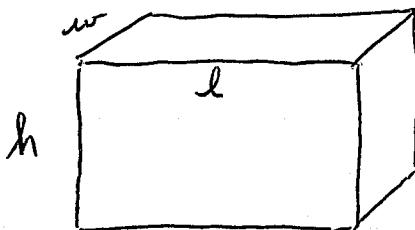
2.



Total distance is  $s = w + l + w + l = 2w + 2l$

$$\begin{aligned} s &= 2(19.5 \text{ m}) + 2(38.44 \text{ m}) = 39.0 \text{ m} + 76.88 \text{ m} \\ &= 115.88 \text{ m} = \boxed{115.9 \text{ m}} \end{aligned}$$

3.



$$\begin{aligned} l &= 50.0 \text{ ft} \\ w &= 26 \text{ ft} \\ h &= 8.0 \text{ ft} \end{aligned}$$

$$\begin{aligned} V &= lwh \\ &= (50.0 \text{ ft})(26 \text{ ft})(8.0 \text{ ft}) \\ &= \underline{10400 \text{ ft}^3} = \underline{10000 \text{ ft}^3} \end{aligned}$$

$$1 \text{ m} = 39.37 \text{ in} = 3.281 \text{ ft}$$

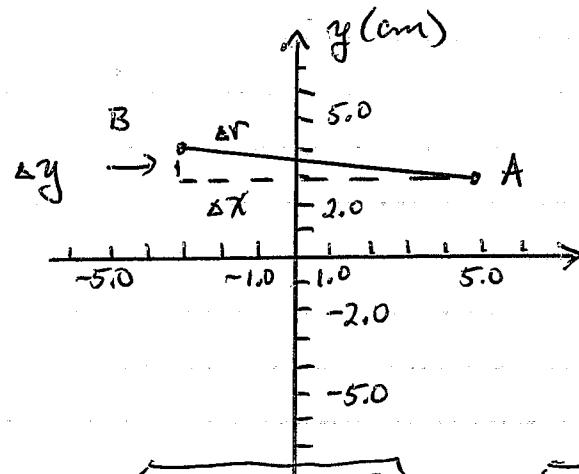
$$\begin{aligned} V &= 10000 \text{ ft}^3 \times \left(\frac{1,000 \text{ m}}{3.281 \text{ ft}}\right)^3 = 283.127 \text{ m}^3 \\ &\quad = \boxed{280 \text{ m}^3} \end{aligned}$$

$$1 \text{ m} = 100 \text{ cm}$$

$$V = 280 \text{ m}^3 \times \left(\frac{100 \text{ cm}}{1 \text{ m}}\right)^3 = \boxed{2.8 \times 10^8 \text{ cm}^3}$$

1-3

4.

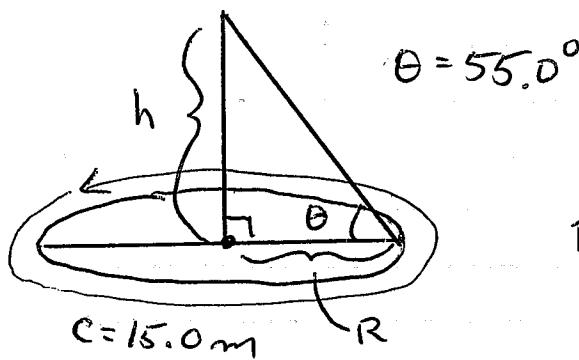


$$\begin{aligned}(\Delta r)^2 &= (\Delta x)^2 + (\Delta y)^2 \\ \Delta x &= x_A - x_B \\ &= 5.0 \text{ cm} - (-3.0 \text{ cm}) \\ &= 8.0 \text{ cm}\end{aligned}$$

$$\begin{aligned}\Delta y &= y_A - y_B \\ &= 3.0 \text{ cm} - 4.0 \text{ cm} \\ &= -1.0 \text{ cm}\end{aligned}$$

$$\begin{aligned}\Delta r &= \sqrt{(\Delta x)^2 + (\Delta y)^2} = \sqrt{(8.0 \text{ cm})^2 + (-1.0 \text{ cm})^2} \\ &= \sqrt{64. \text{ cm}^2 + 1.0 \text{ cm}^2} = \sqrt{65 \text{ cm}^2} = \boxed{8.1 \text{ cm}}\end{aligned}$$

5.



$C = \text{circumference}$   
 $= \pi D, D = \text{diameter}$   
 $= 2\pi R, R = \text{radius}$

$$R = \frac{C}{2\pi} = \frac{15.0 \text{ m}}{2\pi} = 2.39 \text{ m}$$

$h = \text{height}$

$$\text{Note that } \tan \theta = \frac{h}{R}$$

$$\text{or } h = R \tan \theta = (2.39 \text{ m}) \tan 55.0^\circ$$

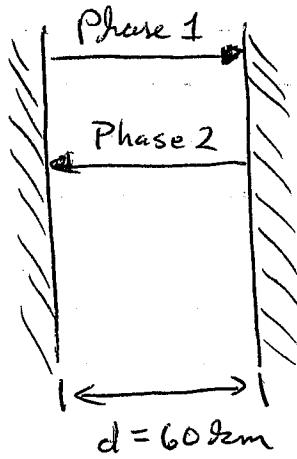
$$= \boxed{3.41 \text{ m}}$$

6.

Phase 1: across lake,  $\bar{v}_{A1} = 60 \frac{\text{km}}{\text{h}}$ ,  $\bar{v}_{B1} = 30 \frac{\text{km}}{\text{h}}$   
 (+x dir)

Phase 2: return,  $\bar{v}_{A2} = -60 \frac{\text{km}}{\text{h}}$ ,  $\bar{v}_{B2} = -90 \frac{\text{km}}{\text{h}}$   
 (-x dir)

a)



$$t = \frac{d}{\bar{v}}$$

$$t_{A1} = \frac{60 \text{ km}}{60 \frac{\text{km}}{\text{h}}} = 1.0 \text{ h}$$

$$t_{B1} = \frac{60 \text{ km}}{30 \frac{\text{km}}{\text{h}}} = 2.0 \text{ h}$$

$$t_{A2} = \frac{60 \text{ km}}{60 \frac{\text{km}}{\text{h}}} = 1.0 \text{ h}$$

$$t_{B2} = \frac{60 \text{ km}}{90 \frac{\text{km}}{\text{h}}} = \frac{2}{3} \text{ h} = 0.67 \text{ h}$$

$$t_A = t_{A1} + t_{A2} = 2.0 \text{ h}, \quad t_B = t_{B1} + t_{B2} = 2.7 \text{ h}$$

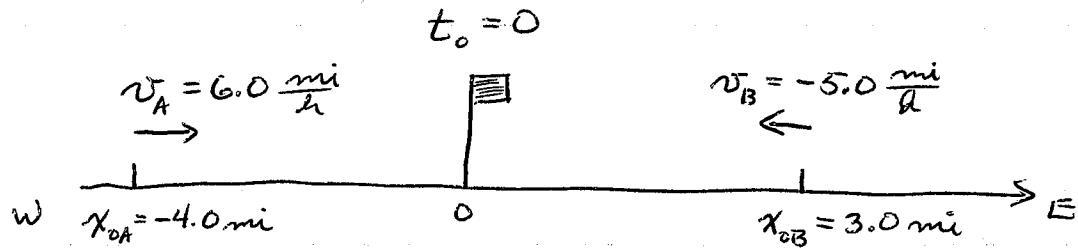
$t_A < t_B$ , boat A wins! by  $\Delta t = t_B - t_A = 0.7 \text{ h}$   
 and distance of 60 km

b)  $\bar{v}_A = \frac{\bar{v}_{A1} + \bar{v}_{A2}}{2} = \frac{60 \frac{\text{km}}{\text{h}} - 60 \frac{\text{km}}{\text{h}}}{2} = \boxed{0}$

or by calculating displacement over time:

$$\bar{v}_A = \frac{x_{A1} + x_{A2}}{t_{A1} + t_{A2}} = \frac{60 \text{ km} - 60 \text{ km}}{2.0 \text{ hr}} = 0 \checkmark$$

7.



$$x_A = x_{oA} + v_A t, \quad x_B = x_{oB} + v_B t$$

$$\text{Find } t \text{ when } x_A = x_B: \quad x_{oA} + v_A t = x_{oB} + v_B t$$

$$\begin{aligned} v_A t - v_B t &= x_{oB} - x_{oA} \\ (v_A - v_B) t &= x_{oB} - x_{oA} \end{aligned}$$

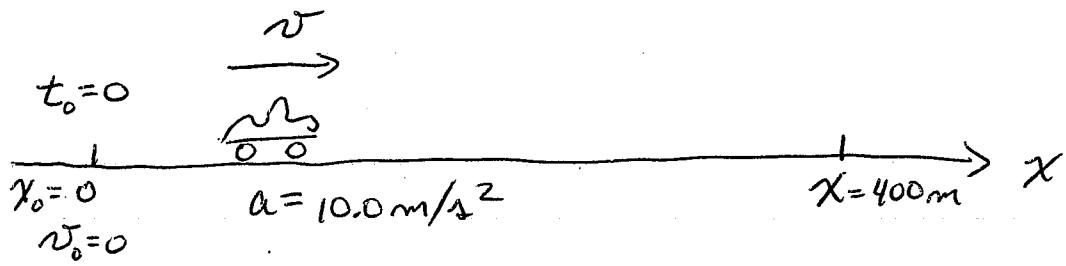
$$t = \frac{x_{oB} - x_{oA}}{v_A - v_B} = \frac{3.0 \text{ mi} - (-4.0 \text{ mi})}{6.0 \frac{\text{mi}}{\text{h}} - (-5.0 \frac{\text{mi}}{\text{h}})} = \frac{7.0 \text{ mi}}{11.0 \frac{\text{mi}}{\text{h}}}$$

= 0.63636 hr (Keep extra digits to avoid round-off error below)

$$\begin{aligned} \text{Final position: } x_A &= x_{oA} + v_A t = -4.0 \text{ mi} + (6.0 \frac{\text{mi}}{\text{h}}) \times \\ &\quad (0.63636 \text{ hr}) \\ &= -0.18 \text{ mi} \end{aligned}$$

\$x\_s = 0.18 \text{ mi W of flagpole.}\$

8.



a) Time to get to  $x = 400 \text{ m}$ :

$$\text{We can use: } x = x_0 + v_0 t + \frac{1}{2} a t^2$$

where  $v_0 = 0$  (starts from rest) and  $x_0 = 0$ .

$$\text{Now, solve for } t: \quad x = 0 + 0 + \frac{1}{2} a t^2$$

$$t^2 = \frac{2x}{a}$$

$$t = \sqrt{\frac{2x}{a}} = \sqrt{\frac{2(400 \text{ m})}{10.0 \text{ m/s}^2}}$$

$$= \sqrt{80.0 \text{ s}^2} = \boxed{8.94 \text{ s}}$$

b) Need  $v$  at  $x = 400 \text{ m}$ :

$$\text{Use: } v = v_0 + a t = 0 + a t$$

$$v = (10.0 \frac{\text{m}}{\text{s}^2})(8.94 \text{ s}) = \boxed{89.4 \text{ m/s}}$$

9.

During Phase 2, we have

$$y_2 = y_1 + v_i(t_2 - t_1) - \frac{1}{2}g(t_2 - t_1)^2$$

$$t_2 - t_1 = 1.50\text{s}, y_2 = 0$$

$$y_1 = 30.0\text{ m}$$

$$0 = y_1 + v_i(t_2 - t_1) - \frac{1}{2}g(t_2 - t_1)^2$$

$$v_i(t_2 - t_1) = -y_1 + \frac{1}{2}g(t_2 - t_1)^2$$

$$v_i = -\frac{y_1}{(t_2 - t_1)} + \frac{g}{2}(t_2 - t_1)$$

$$= -\frac{30.0\text{ m}}{1.50\text{s}} + \frac{9.80\text{ m/s}^2}{2}(1.50\text{s}) = -20.0\frac{\text{m}}{\text{s}} + 7.35\frac{\text{m}}{\text{s}}$$

$$= -12.65\frac{\text{m}}{\text{s}} = -12.7\frac{\text{m}}{\text{s}}$$

During Phase 1, we have

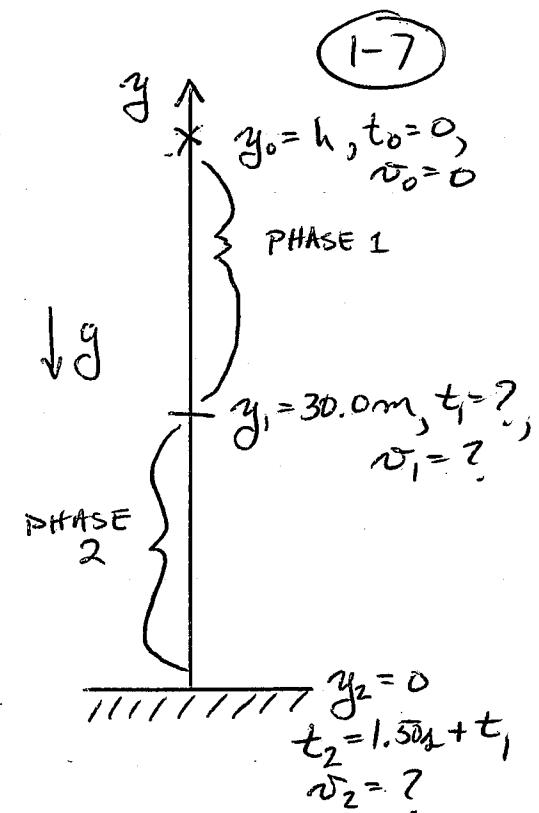
$$v_i^2 = v_0^2 - 2g(y_1 - y_0), v_0 = 0, y_0 = h$$

$$2g(y_1 - h) = -v_i^2, y_1 - h = -\frac{v_i^2}{2g}$$

$$h = y_1 + \frac{v_i^2}{2g} = 30.0\text{ m} + \frac{(-12.7\frac{\text{m}}{\text{s}})^2}{2(9.80\text{ m/s}^2)}$$

$$= 30.0\text{ m} + 8.16\text{ m} = 38.16\text{ m}$$

$$= \boxed{38.2\text{ m}}$$



1-7

10.

Label Kathy variables with a 'K' and Sam variables with an 'S', then our given parameters are

$$a_K = 4.90 \frac{m}{s^2}, v_{0K} = 0 \frac{m}{s}, t_{0K} = 0 s, x_{0K} = 0 m$$

$$a_S = 3.50 \frac{m}{s^2}, v_{0S} = 0 \frac{m}{s}, t_{0S} = -1.00 s, x_{0S} = 0 m$$

a) Determine the time when  $x_K = x_S$ :

$$\begin{aligned} x_K &= x_{0K} + v_{0K}(t - t_{0K}) + \frac{1}{2} a_K (t - t_{0K})^2 \\ &= 0 + 0 + \frac{1}{2} a_K (t - 0)^2 = \frac{1}{2} a_K t^2 \end{aligned}$$

$$\begin{aligned} x_S &= x_{0S} + v_{0S}(t - t_{0S}) + \frac{1}{2} a_S (t - t_{0S})^2 \\ &= 0 + 0 + \frac{1}{2} a_S (t - t_{0S})^2 = \frac{1}{2} a_S (t - t_{0S})^2 \end{aligned}$$

Now,

$$x_K = x_S$$

$$\frac{1}{2} a_K t^2 = \frac{1}{2} a_S (t - t_{0S})^2$$

$$a_K t^2 = a_S (t - t_{0S})^2$$

Take square-root of both sides:

$$\sqrt{a_K} t = \sqrt{a_S} (t - t_{0S})$$

1-9

Now solve for  $t$ :

$$\sqrt{a_k} t - \sqrt{a_s} t = -\sqrt{a_s} t_{0s}$$

$$(\sqrt{a_k} - \sqrt{a_s}) t = -\sqrt{a_s} t_{0s}$$

$$t = -\frac{\sqrt{a_s}}{(\sqrt{a_k} - \sqrt{a_s})} t_{0s}$$

$$= -\frac{\sqrt{3.50 \text{ m/s}^2}}{(\sqrt{4.90 \text{ m/s}^2} - \sqrt{3.50 \text{ m/s}^2})} (-1.00 \text{ s})$$

$$= \frac{1.87}{0.343} (1.00 \text{ s}) = \boxed{5.46 \text{ s}}$$

They meet 5.46 s after Kathy starts.

b) Distance traveled when  $x_k = x_s$ :

$$x_s = x_k = \frac{1}{2} a_k t^2 = \frac{1}{2} (4.90 \frac{\text{m}}{\text{s}^2}) (5.46 \text{ s})^2$$

$$= \boxed{73.0 \text{ m}}$$

c) Find  $v_k$  and  $v_s$  when  $x_k = x_s$ :

$$v_k = v_{0k} + a_k(t - t_{0k})$$

$$= 0 + a_k(t - 0) = a_k t$$

$$v_k = (4.90 \frac{m}{s^2})(5.46 s) = \boxed{26.8 \frac{m}{s}}$$

1-10

$$v_s = v_{os} + a_s(t - t_{os})$$

$$= 0 + (3.50 \frac{m}{s^2})(5.46 s - (-1.00 s))$$

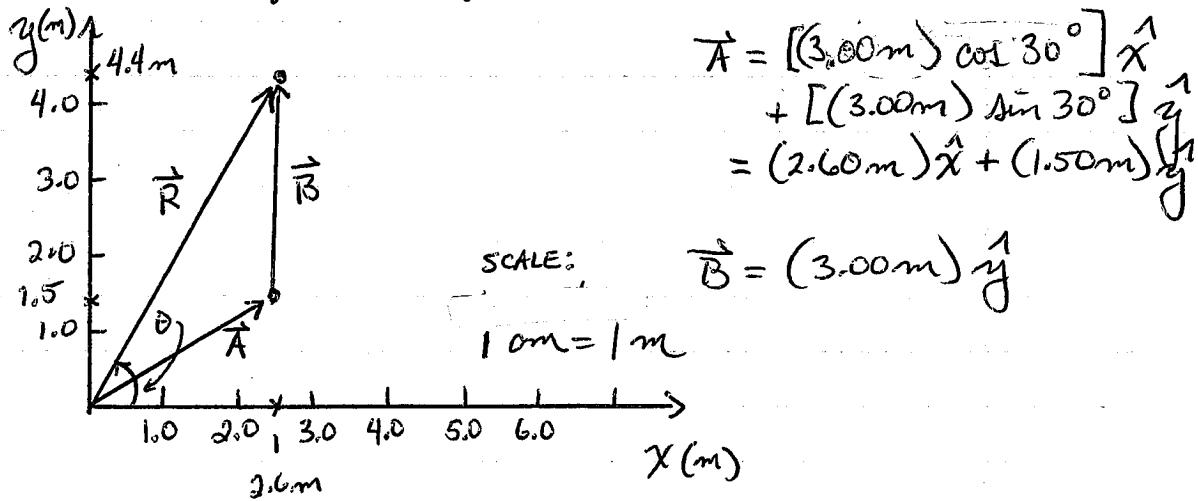
$$= (3.50 \frac{m}{s^2})(6.46 s)$$

$$= \boxed{22.6 \frac{m}{s}}$$

1-11

11.

a)  $\vec{A} + \vec{B}$ : Translate  $\vec{B}$  so that it starts at the end of  $\vec{A}$  for the graphical solution:



Graphically: (measured)  $\vec{R} = (2.6\text{m}) \hat{x} + (4.4\text{m}) \hat{y}$

$$|\vec{R}| = R = 5.1\text{m}, \theta = 60^\circ \text{ (measured)}$$

Algebraically:  $\vec{A} + \vec{B} = (2.60\text{m} + 0\text{m}) \hat{x} + (1.50\text{m} + 3.00\text{m}) \hat{y}$

$$\vec{R} = \vec{A} + \vec{B} = (2.60\text{m}) \hat{x} + (4.50\text{m}) \hat{y}$$

$$R = \sqrt{(2.60\text{m})^2 + (4.50\text{m})^2} = \sqrt{27.01\text{m}^2}$$

$$= \boxed{5.20\text{m}}$$

$$\tan \theta = \frac{R_y}{R_x}, \quad \theta = \tan^{-1} \left( \frac{4.50\text{m}}{2.60\text{m}} \right) = \boxed{60.0^\circ}$$

b)  $\vec{A} - \vec{B}$

Graphically:

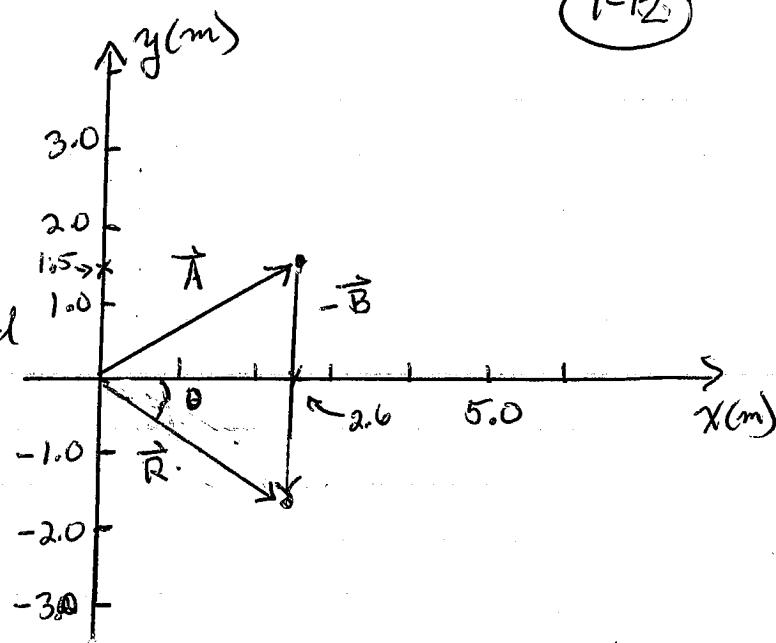
$$R_x = 2.6 \text{ m}$$

$$R_y = -1.6 \text{ m}$$

$$R = 3.1 \text{ m}$$

$$\theta = -30^\circ$$

All measured



Algebraically:

$$\begin{aligned}\vec{R} &= \vec{A} - \vec{B} = (2.60 \text{ m} - 0 \text{ m}) \hat{x} + (1.50 \text{ m} - 3.00 \text{ m}) \hat{y} \\ &= (2.60 \text{ m}) \hat{x} - (1.50 \text{ m}) \hat{y}\end{aligned}$$

$$\begin{aligned}R &= |\vec{R}| = \sqrt{(2.60 \text{ m})^2 + (-1.50 \text{ m})^2} \\ &= \sqrt{9.01 \text{ m}^2} = \boxed{3.00 \text{ m}}\end{aligned}$$

$$\theta = \tan^{-1} \left( \frac{-1.50 \text{ m}}{2.60 \text{ m}} \right) = \boxed{-30.0^\circ} = 330^\circ$$

c)  $\vec{B} - \vec{A}$

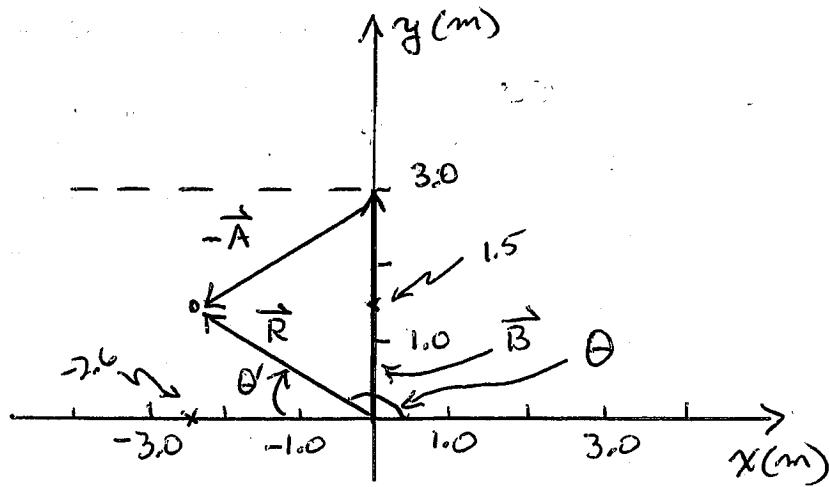
Graphically:

$$R_x = -2.6 \text{ m}$$

$$R_y = 1.5 \text{ m}$$

$$R = 3.0 \text{ m}$$

$$\theta = 150^\circ$$



(1-13)

Algebraically:

$$\vec{R} = \vec{B} - \vec{A} = (0 - 2.60\text{m}) \hat{x} + (3.00\text{m} - 1.50\text{m}) \hat{y} \\ = -(2.60\text{m}) \hat{x} + (1.50\text{m}) \hat{y}$$

$$R = |\vec{R}| = \sqrt{(-2.60\text{m})^2 + (1.50\text{m})^2} = \sqrt{9.01\text{ m}^2} \\ = \boxed{3.00\text{ m}}$$

$$\theta' = \tan^{-1} \frac{R_y}{R_x} = \tan^{-1} \left( \frac{1.50\text{m}}{-2.60\text{m}} \right) = -30.0^\circ$$

Note however that since we are in the 2nd quadrant, this  $\theta$  (marked  $\theta'$  here) is with respect to the  $-x$  axis, the negative sign in  $\theta'$  indicates the angle is clockwise wrt the  $-x$  axis. As such,

$$\theta = 180^\circ + \theta' = 180^\circ - 30.0^\circ = \boxed{150.0^\circ}$$

d)  $\vec{R} = \vec{A} - 2\vec{B}$

Graphically:

$$R_x = 2.6\text{m}$$

$$R_y = -4.5\text{m}$$

$$R = 5.2\text{m}$$

$$\theta = -60^\circ$$

Algebraically:

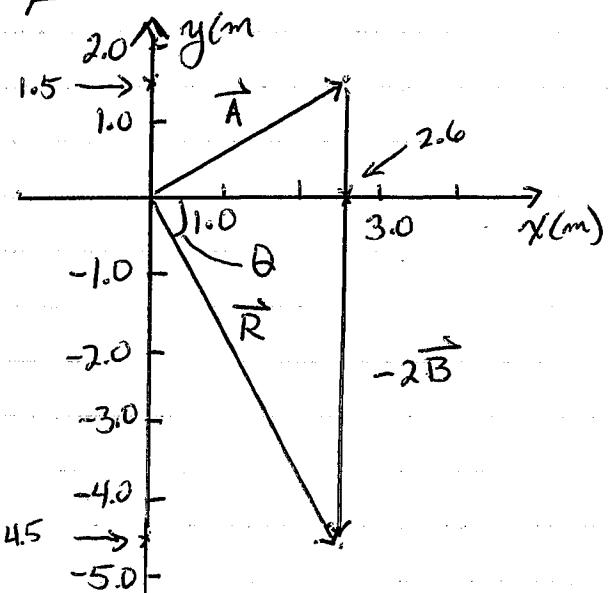
$$\vec{R} = \vec{A} - 2\vec{B} = (2.60\text{m} - 0) \hat{x}$$

$$+ (1.50\text{m} - 2 \times 3.00\text{m}) \hat{y}$$

$$= (2.60\text{m}) \hat{x} - (4.50\text{m}) \hat{y}$$

$$R = \sqrt{(2.60\text{m})^2 + (-4.50\text{m})^2}$$

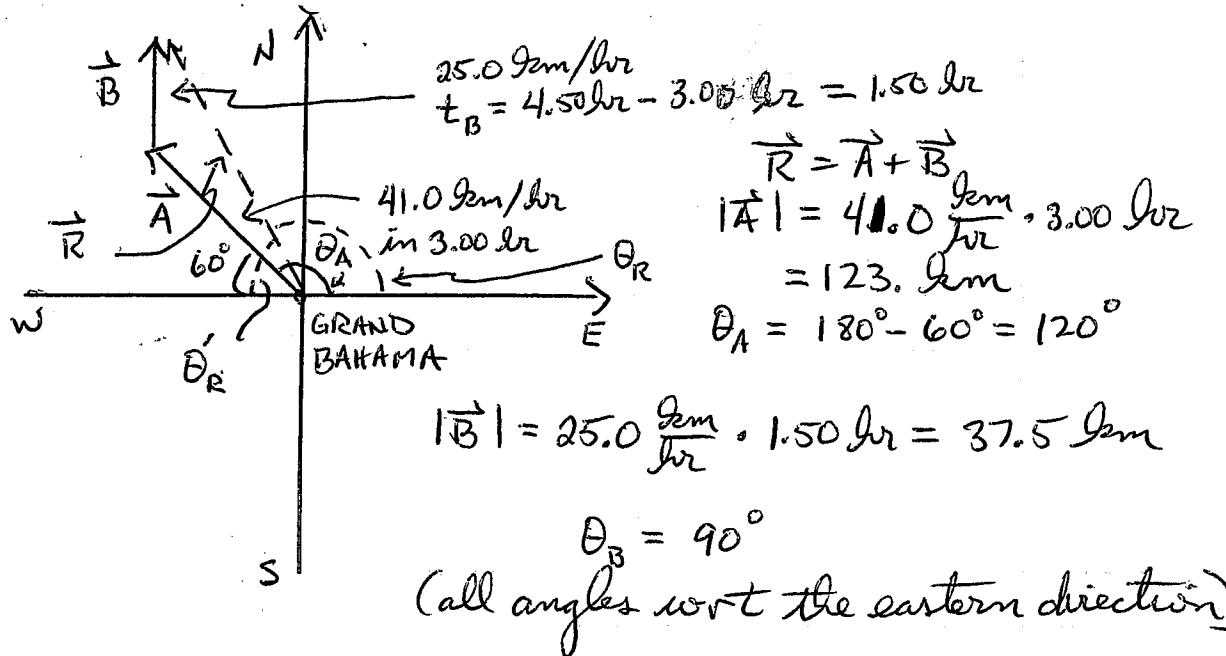
$$= \boxed{5.20\text{ m}}$$



$$\theta = \tan^{-1} \left( \frac{-4.50\text{m}}{2.60\text{m}} \right) = \boxed{-60.0^\circ}$$

1-14

12.



$$\vec{R} = \vec{A} + \vec{B} = (A_x + B_x) \hat{x} + (A_y + B_y) \hat{y}$$

$$A_x = A \cos \theta_A = (123 \text{ km}) \cos 120^\circ = -61.5 \text{ km}$$

$$A_y = A \sin \theta_A = (123 \text{ km}) \sin 120^\circ = 106.5 \text{ km}$$

$$B_x = 0, \quad B_y = B = 37.5 \text{ km}$$

$$\begin{aligned} \vec{R} &= (-61.5 \text{ km} + 0) \hat{x} + (106.5 \text{ km} + 37.5 \text{ km}) \hat{y} \\ &= -(61.5 \text{ km}) \hat{x} + (144 \text{ km}) \hat{y} \end{aligned}$$

$$R = \sqrt{(-61.5 \text{ km})^2 + (144 \text{ km})^2} = \boxed{157 \text{ km}} \quad \text{NW of Grand Bahama}$$

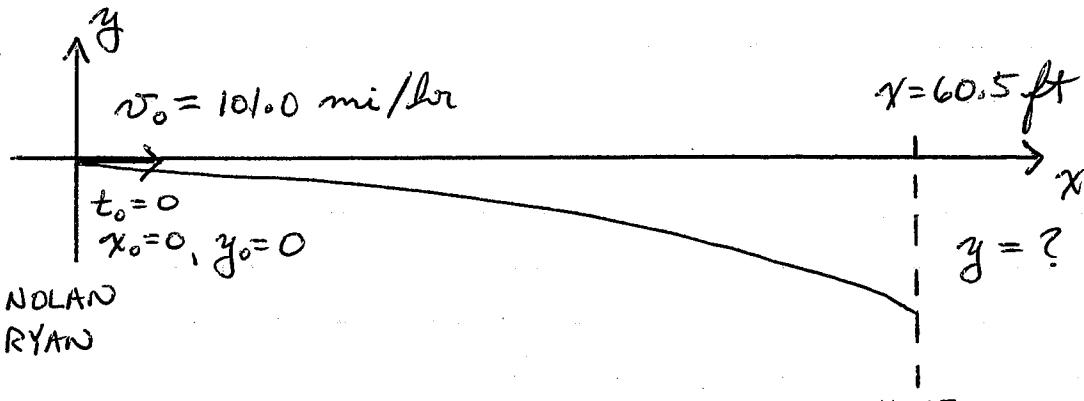
$$\theta'_R = \tan^{-1} \left( \frac{R_y}{R_x} \right) = \tan^{-1} \left( \frac{144 \text{ km}}{-61.5 \text{ km}} \right) = -66.9^\circ \quad (\text{from the } -x \text{ or W direction})$$

$$\theta_R = 180^\circ + \theta'_R = 180^\circ - 66.9^\circ = \boxed{113^\circ} \quad \text{from E direction}$$

or  
 $67^\circ \text{ N of W from Grand Bahama}$

(1-15)

13.



NOLAN

RYAN

$$\begin{aligned}\overrightarrow{v_{0x}} &= \overrightarrow{v_0} = \left(101.0 \frac{\text{mi}}{\text{hr}}\right) \hat{x} \\ &= \left(101.0 \frac{\text{mi}}{\text{hr}} \times 5280 \frac{\text{ft}}{\text{mi}} \times \frac{1 \text{ hr}}{3600 \text{ s}}\right) \hat{x} \\ &= (148.1 \text{ ft/s}) \hat{x}\end{aligned}$$

$$\overrightarrow{v_{0y}} = 0$$

Since there is no acceleration in the  $x$ -direction,

$$x = x_0 + v_{0x} t = v_{0x} t, \text{ or } t = \frac{x}{v_{0x}} = \frac{60.5 \text{ ft}}{148.1 \text{ ft/s}} = 0.409 \text{ s}$$

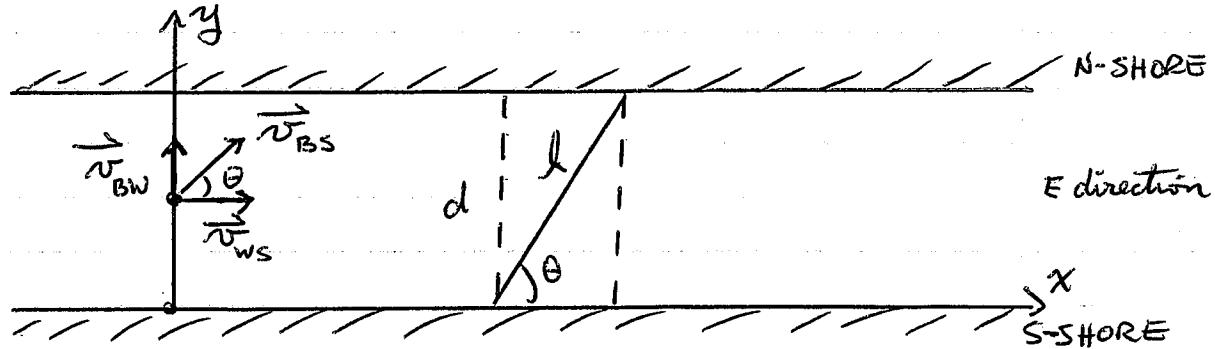
Now we

$$\begin{aligned}y &= y_0 + v_{0y} t - \frac{1}{2} g t^2 = 0 + 0 - \frac{1}{2} (32.0 \frac{\text{ft}}{\text{s}^2}) (0.409 \text{ s})^2 \\ &= \boxed{-2.68 \text{ ft}}\end{aligned}$$

The ball drops 2.68 ft from the  $y$  position that Billy Wagner pitches it.

1-16

14



Let  $\vec{v}_{BW}$  be the velocity of the boat wrt the water,

$\vec{v}_{WS}$  " " " " water " " shore,

$\vec{v}_{BS}$  " " " " boat " " shore.

a) Find  $\vec{v}_{BS}$ :

$$\vec{v}_{BS} = \vec{v}_{WS} + \vec{v}_{BW}$$

$$\vec{v}_{WS} = (1.50 \text{ m/s}) \hat{x} \quad (\text{east direction})$$

$$\vec{v}_{BW} = (10.0 \text{ m/s}) \hat{y} \quad (\text{north direction})$$

$$\vec{v}_{BS} = (1.50 \text{ m/s}) \hat{x} + (10.0 \text{ m/s}) \hat{y}$$

$$\begin{aligned} v_{BS} &= |\vec{v}_{BS}| = \sqrt{v_x^2 + v_y^2} = \sqrt{(1.50 \frac{\text{m}}{\text{s}})^2 + (10.0 \frac{\text{m}}{\text{s}})^2} \\ &= \sqrt{(102.25 \text{ m}^2/\text{s}^2)} = \boxed{10.1 \frac{\text{m}}{\text{s}}} \end{aligned}$$

$\theta$  = angle wrt south shore, so

$$\theta = \tan^{-1} \left( \frac{v_y}{v_x} \right) = \tan^{-1} \left( \frac{10.0 \text{ m/s}}{1.50 \text{ m/s}} \right)$$

$= \tan^{-1}(6.667) = 81.5^\circ$  wrt the south shore

or  $90^\circ - 81.5^\circ = \boxed{8.5^\circ \text{ E of the N direction}}$

- b) Let  $l$  be the actual path the boat travels across the river and  $d$  be the width of the river, then

$\sin \theta = \frac{d}{l}$  where this  $\theta$  is the same  $\theta$  as calculated with the velocity vectors

$$l = \frac{d}{\sin \theta} = \frac{300. \text{ m}}{\sin 81.5^\circ} = 303 \text{ m}$$

The time to cross the river is found from

$$v_{BS} = l/t \text{ or } t = l/v_{BS} = 303 \text{ m} / 10.1 \text{ m/s} = 30.0 \text{ s}$$

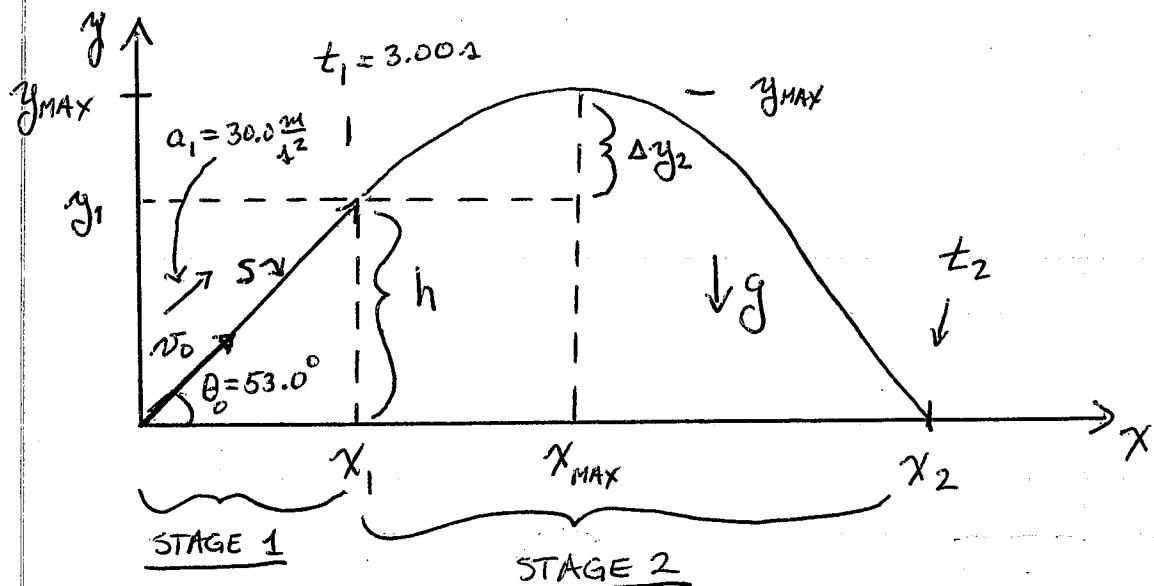
Let  $x$  be the eastward displacement that the boat experiences as it crosses the river, then

$$x = v_{BSx} t = v_{ws} t = (1.50 \frac{\text{m}}{\text{s}})(30.0 \text{ s})$$

$\uparrow$   $x$ -component of  $v_{BS}$

$\boxed{x = 45.1 \text{ m}}$

15.



a) Find  $y_{\text{MAX}}$ :

Break problem into 2 stages:

During stage 1, the total acceleration of the rocket is in the same direction as  $\vec{v}_0$ . During this stage, the rocket moves a distance  $s$  along the direction of  $\vec{v}_0$ :

$$s = v_0 t_1 + \frac{1}{2} a_1 t_1^2, \text{ where } v_0 = 100 \frac{\text{m}}{\text{s}},$$

$$a_1 = 30.0 \frac{\text{m}}{\text{s}^2}, \text{ and } t_1 = 3.00\text{ s}:$$

$$s = (100 \frac{\text{m}}{\text{s}})(3.00\text{ s}) + \frac{1}{2} (30.0 \frac{\text{m}}{\text{s}^2})(3.00\text{ s})^2$$

$$= 300 \frac{\text{m}}{\text{s}} + 135 \text{ m} = 435 \text{ m}$$

1-19

At this time, its location is  $x_1$ , where

$$x_1 = s \cos \theta_0 = (435. \text{ m}) \cos 53.0^\circ = 262. \text{ m}.$$

Its vertical height is

$$y_1 = h = s \sin \theta_0 = (435. \text{ m}) \sin 53.0^\circ = 347. \text{ m}$$

and its velocity at that point is

$$\begin{aligned} v_1 &= v_0 + at = 100. \frac{\text{m}}{\text{s}} + (30.0 \frac{\text{m}}{\text{s}^2})(3.00 \text{ s}) \\ &= 190. \text{ m/s} \end{aligned}$$

in the same direction as  $\vec{v}_0$ . This acts as a new initial velocity for stage 2. Breaking this velocity into its  $x$  &  $y$  components give

$$v_{1x} = v_1 \cos \theta_0 = (190. \frac{\text{m}}{\text{s}}) \cos 53.0^\circ = 114. \frac{\text{m}}{\text{s}}$$

$$v_{1y} = v_1 \sin \theta_0 = (190. \frac{\text{m}}{\text{s}}) \sin 53.0^\circ = 152. \frac{\text{m}}{\text{s}}$$

At the maximum height,  $v_y^{\max}$ ,  $v_y = 0$ . Realizing that the acceleration during this stage (i.e., stage 2) is

$$\vec{a}_2 = -g \hat{j} \quad \text{and} \quad v_{20} = v_1 \quad \text{so}$$

$$v_y = v_{1y} + a_2 t \quad \text{or} \quad 0 = v_{1y} - g t$$

Solving for  $t$  gives:

$$t = \frac{v_{1y}}{g} = \frac{152 \text{ m/s}}{9.80 \text{ m/s}^2} = 15.5 \text{ s}$$

→ however this is the time since  $t_1$ !

$$\text{So } t_{\text{MAX}} = t_1 + t = 3.00 \text{ s} + 15.5 \text{ s} = 18.5 \text{ s}$$

Now  $\Delta y_2$  is the additional altitude that the rocket gains from  $h$  at the end of stage 1 to get to  $y_{\text{MAX}}$ , hence we use  $x_1, y_1$ , and  $t_1$  as our initial conditions to get

$$\begin{aligned}\Delta y_2 &= v_{1y} t + \frac{1}{2} a_2 t^2 = v_{1y} t - \frac{1}{2} g t^2 \\ &= (152 \frac{\text{m}}{\text{s}})(15.5 \text{ s}) - \frac{1}{2}(9.80 \frac{\text{m}}{\text{s}^2})(15.5 \text{ s})^2 \\ &= 2348 \text{ m} - 1174 \text{ m} = 1174 \text{ m}\end{aligned}$$

So the maximum height above the ground is

$$\begin{aligned}y_{\text{MAX}} &= h + \Delta y_2 = 347 \text{ m} + 1174 \text{ m} = 1521 \text{ m} \\ &= \boxed{1521 \text{ m}}\end{aligned}$$

We will refer to the time from  $t_1$  until the rocket gets to  $y_{\text{MAX}}$  as

$$t_* = 15.5 \text{ s}$$

for the rest of this problem.

1-21

b) Total flight time:

We need to figure out how long it will take for the rocket to fall to the ground from  $y_{MAX}$ . Let's label this time as  $t_f$ , then

$$t_2 = t_* + t_f \quad \text{and} \quad t_{TOT} = t_0 + t_1 + t_2 = t_1 + t_* + t_f$$

since the initial time  $t_0 = 0$ . <sup>↗</sup> STAGES

Let  $v_0$  now represent the velocity when the rocket is at  $y_{MAX}$ , then define

$$\Delta y = y_{GROUND} - y_{MAX} = v_{0y} t_f - \frac{1}{2} g t_f^2$$

$$v_{0y} = 0 \quad (\text{top of trajectory}), \quad y_{GROUND} = 0,$$

$$y_{MAX} = 1520 \text{ m}, \text{ so}$$

$$0 - 1520 \text{ m} = 0 - \frac{1}{2} (9.80 \frac{\text{m}}{\text{s}^2}) t_f^2$$

$$\frac{1}{2} (9.80 \frac{\text{m}}{\text{s}^2}) t_f^2 = 1520 \text{ m}$$

$$t_f = \sqrt{\frac{1520 \text{ m} \times 2}{9.80 \frac{\text{m}}{\text{s}^2}}} = 17.6 \text{ s}$$

Finally,

$$t_{TOT} = t_1 + t_* + t_f = 3.00 \text{ s} + 15.5 \text{ s} + 17.6 \text{ s}$$

$$= \boxed{36.1 \text{ s}}$$

c) Horizontal range:

The horizontal range during free-fall from  $x_1$  is

$$\Delta x_2 = v_{ix} t_2$$

where  $v_{ix}$  is the (initial) velocity of stage 2 (the free-fall stage) and  $t_2$  (the free fall time) is

$$t_2 = t_* + t_s = 15.5\text{ s} + 17.6\text{ s} = 33.1\text{ s}$$

So

$$\Delta x_2 = (114 \text{ m/s})(33.1 \text{ s}) = 3770 \text{ m}$$

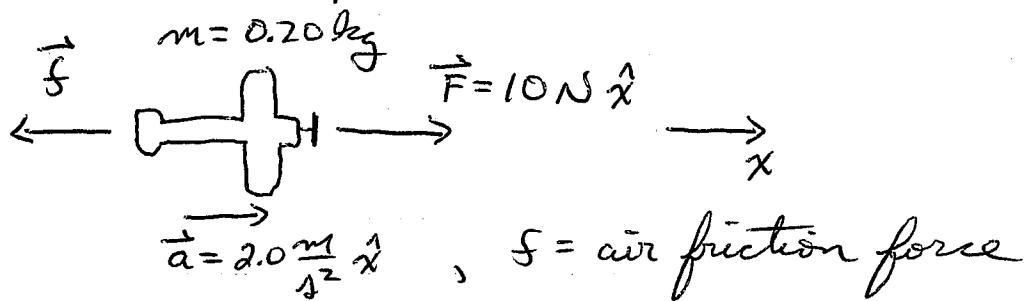
Finally, the total horizontal range is

$$x_2 = x_1 + \Delta x_2 = 262 \text{ m} + 3770 \text{ m}$$

$$= \boxed{4032 \text{ m/s}}$$

1-23

16.



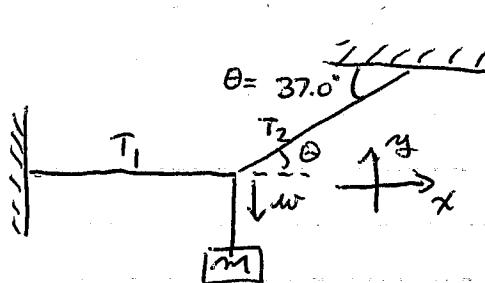
Using Newton's 2nd Law:  $\sum F_x = ma$

$$F - f = ma$$

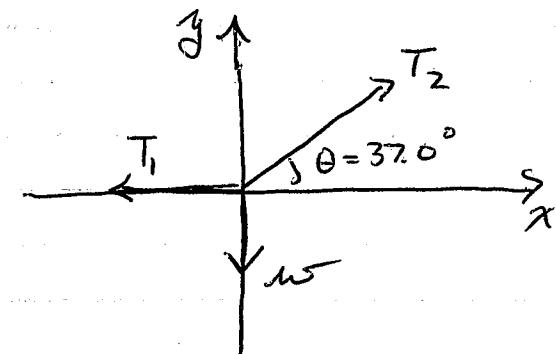
$$f = F - ma = 10 \text{ N} - (0.20 \text{ kg})(2.0 \frac{\text{m}}{\text{s}^2})$$

$$= 10 \text{ N} - 0.4 \text{ N} = \boxed{9.6 \text{ N}}$$

17.



$$w = mg = 600 \text{ N}$$



Equilibrium is effect:  $\sum F_y = T_2 \sin \theta - w = 0$

$$T_2 = \frac{w}{\sin \theta} = \frac{600 \text{ N}}{\sin 37.0^\circ} = \boxed{997 \text{ N}}$$

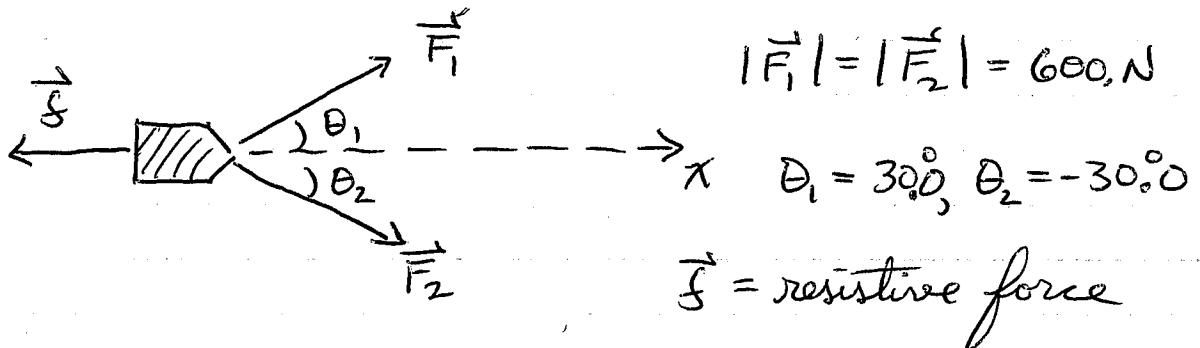
inclined cable

$$\sum F_x = T_2 \cos \theta - T_1 = 0$$

$$T_1 = T_2 \cos \theta = (997 \text{ N}) \cos 37.0^\circ = \boxed{796 \text{ N}}$$

horizontal cable

18.



Since boat moves at constant velocity,  $\vec{a}_{\text{BOAT}} = 0$ .

$\therefore \sum \vec{F} = m\vec{a} = 0$ :

$$\sum \vec{F} = \vec{F}_1 + \vec{F}_2 + \vec{f} = 0$$

Only need to work in  $x$ -direction:

$$\sum F_x = F_1 \cos \theta_1 + F_2 \cos \theta_2 - f = 0$$

$$f = F_1 \cos \theta_1 + F_2 \cos \theta_2$$

$$= (600 \text{ N}) \cos 30.0^\circ + (600 \text{ N}) \cos (-30.0^\circ)$$

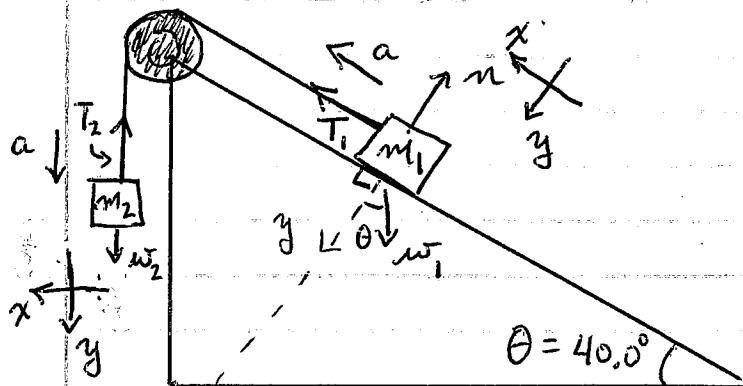
$$= 520 \text{ N} + 520 \text{ N} = 1040 \text{ N}$$

Since  $f$  is pointed in the negative  $x$  direction,

$$\boxed{\vec{f} = (-1040 \text{ N}) \hat{x}}$$

1-25

19.



$$m_1 = 5.00 \text{ kg}$$

$$m_2 = 10.0 \text{ kg}$$

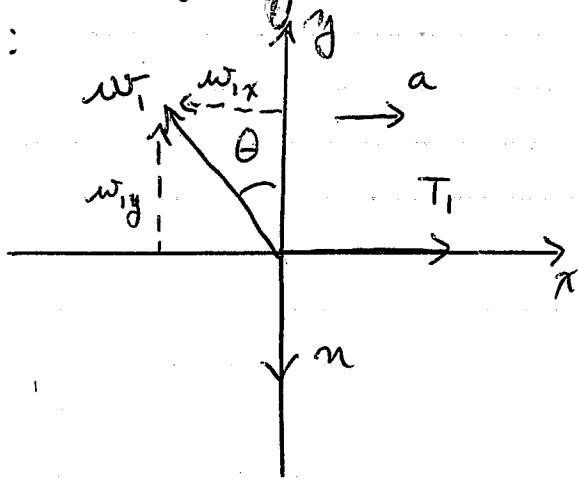
$$m_1 < m_2$$

$$\theta = 40.0^\circ, f_k = 0$$

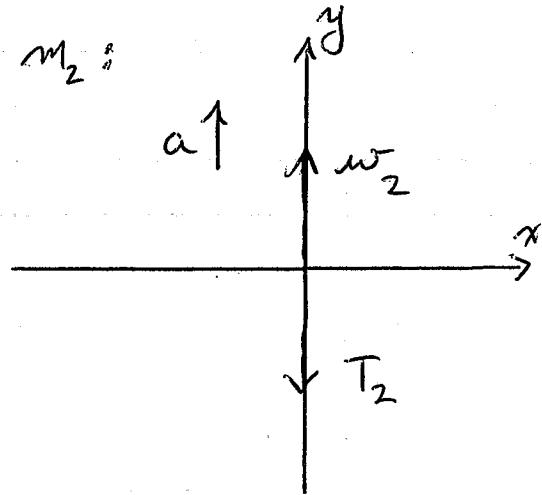
acc. 'a' is same magnitude for both masses.

Free-body diagrams:

$m_1$ :



$m_2$ :



Coordinates chosen such that 'a' points in + dir.

Assume that the string doesn't stretch, then  
 $|\vec{T}_1| = |\vec{T}_2| = T$ .

Mass 1:

$$\sum F_x = T - w_1 \sin \theta = m_1 a \quad (1)$$

$$\sum F_y = w_1 \cos \theta - n = 0 \quad (2)$$

Mass 2:

$$\sum F_y = w_2 - T = m_2 a \quad (3)$$

(no  $x$ -component in force equation)

$$w_1 = m_1 g = (5.00 \text{ kg}) (9.80 \frac{\text{m}}{\text{s}^2}) = 49.0 \text{ N}$$

$$w_2 = m_2 g = (10.0 \text{ kg}) (9.80 \frac{\text{m}}{\text{s}^2}) = 98.0 \text{ N}$$

Solve Eqs. (1) & (3) for ' $a$ ' and subtract:

$$(1): \quad a = \frac{T - m_1 g \sin \theta}{m_1} = \frac{T}{m_1} - g \sin \theta \quad (1^*)$$

$$(3): \quad a = \frac{m_2 g - T}{m_2} = g - \frac{T}{m_2} \quad (3^*)$$


---

$$(1^*) - (3^*): \quad 0 = \frac{T}{m_1} - g \sin \theta - g + \frac{T}{m_2}$$

$$\frac{T}{m_1} + \frac{T}{m_2} = g(1 + \sin \theta)$$

$$T \left( \frac{m_2}{m_1 m_2} + \frac{m_1}{m_1 m_2} \right) = g(1 + \sin \theta)$$

$$\frac{m_1 + m_2}{m_1 m_2} T = g(1 + \sin \theta)$$

$$T = \frac{m_1 m_2}{m_1 + m_2} g (1 + \sin \theta)$$

$$= \frac{(50.0 \text{ kg})^2}{15.0 \text{ kg}} (9.80 \frac{\text{m}}{\text{s}^2}) (1 + \sin 40.0^\circ)$$

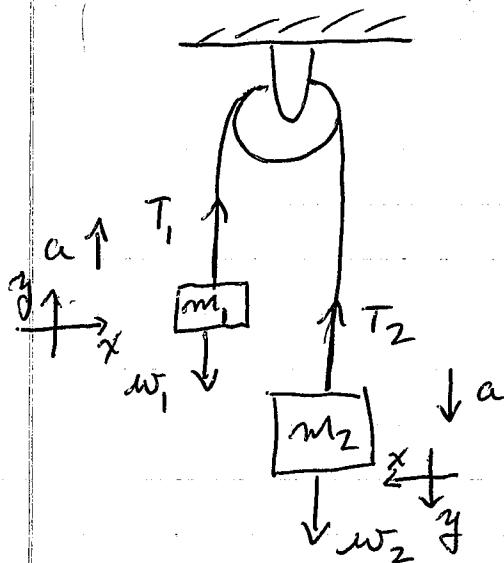
$$= \boxed{53.7 \text{ N}}$$

1-27

Use this in Eq. (3):

$$a = g - \frac{T}{m_2} = 9.80 \frac{m}{s^2} - \frac{53.7 N}{10.0 \text{ kg}}$$
$$= \boxed{4.43 \frac{m}{s^2}}$$

20.



$$m_1 = 3.00 \text{ kg} \quad w_1 = m_1 g$$

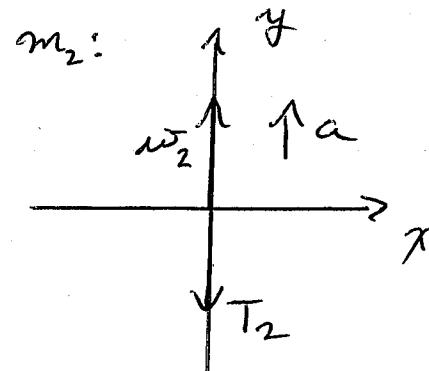
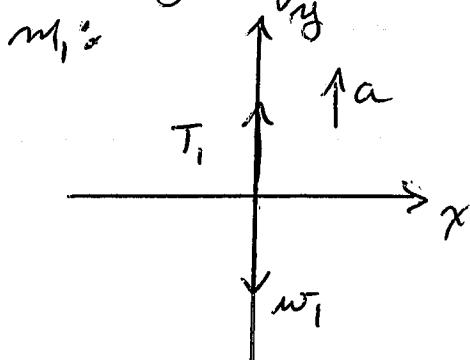
$$m_2 = 5.00 \text{ kg} \quad w_2 = m_2 g$$

$m_2 > m_1$ , so 'a' is in direction indicated and its magnitude will be the same for each mass

Assume string doesn't stretch:

$$|T_1| = |T_2| = T$$

Free-body diagrams:



$$\text{Mass 1: } \sum F_y = T - m_1 g = m_1 a \quad (1)$$

$$\text{Mass 2: } \sum F_y = m_2 g - T = m_2 a \quad (2)$$

a) Find T:

$$a = \frac{T - m_1 g}{m_1} = \frac{T}{m_1} - g \quad (1^*)$$

$$a = \frac{m_2 g - T}{m_2} = g - \frac{T}{m_2} \quad (2^*)$$

$$(1^*) - (2^*): 0 = \frac{T}{m_1} - g - g + \frac{T}{m_2}$$

$$\frac{T}{m_1} + \frac{T}{m_2} = g + g = 2g$$

$$T \left( \frac{m_2 + m_1}{m_1 m_2} \right) = 2g$$

$$T = 2 \frac{m_1 m_2}{m_1 + m_2} g = 2 \left( \frac{15.0 \text{ kg}}{8.00 \text{ kg}} \right) (9.80 \frac{\text{m}}{\text{s}^2})$$

$$= \boxed{36.8 \text{ N}}$$

b) Find acceleration (same for both):

$$T = m_1 a + m_1 g = m_1 (a+g) \quad (1^{**})$$

$$T = m_2 g - m_2 a = m_2 (g-a) \quad (2^{**})$$

$$(1^{**}) - (2^{**}): 0 = m_1 (a+g) - m_2 (g-a)$$

$$0 = m_1 a + m_1 g - m_2 g + m_2 a$$

$$= a(m_1 + m_2) + g(m_1 - m_2)$$

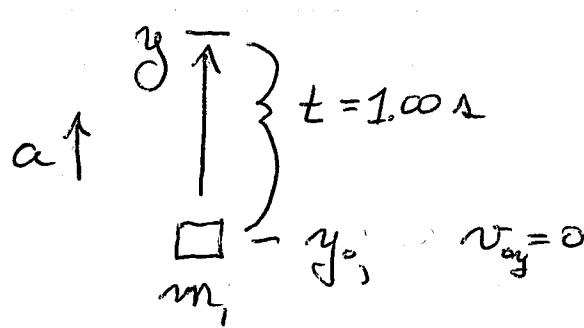
$$a = -g \frac{(m_1 - m_2)}{(m_1 + m_2)} = \frac{m_2 - m_1}{m_1 + m_2} g$$

$$= \frac{2.00 \text{ kg}}{8.00 \text{ kg}} (9.80 \text{ m/s}^2) = \boxed{2.45 \text{ m/s}^2}$$

1-30

c) Find  $\Delta y$  (same for both) in 1 second:

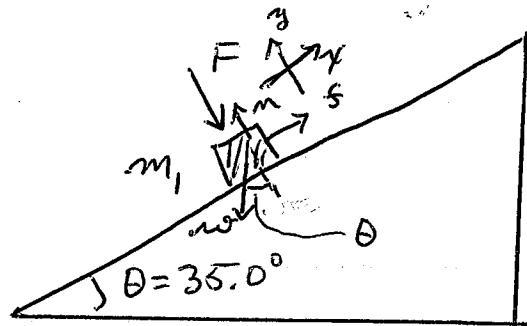
Since  $\Delta y$  will be the same for both masses, we will choose to work with  $m_1$ :



$$\begin{aligned}y &= y_0 + v_{0y} t + \frac{1}{2} a t^2 \\ \Delta y &= v_{0y} t + \frac{1}{2} a t^2 \\ &= 0 + \frac{1}{2} (2.45 \frac{\text{m}}{\text{s}^2}) (1.00\text{ s})^2 \\ &= \boxed{1.23\text{ m}}\end{aligned}$$

1-31

21.



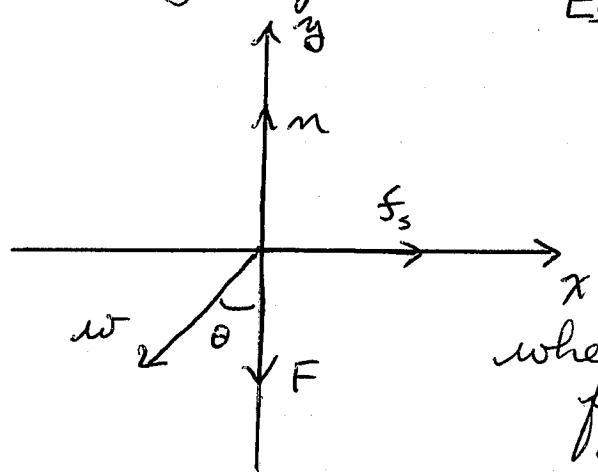
$$\mu_s = 0.300$$

$$m_1 = 3.00 \text{ kg}$$

$$\theta = 35.0^\circ$$

Minimum  $F$  to prevent block from sliding:

Free-body diagram:



Equilibrium applies:

$$\sum F_x = f_s - w \sin \theta = 0$$

$$\sum F_y = n - F - w \cos \theta = 0$$

where, here,  $F$  is the minimum force to just keep mass from sliding and  $w = mg$ .

$$\text{From } y: F = n - w \cos \theta \quad (1)$$

$$\text{From } x: f_s = \mu_s n = w \sin \theta \quad (2)$$

$$\text{so } n = \frac{w \sin \theta}{\mu_s} = \frac{mg \sin \theta}{\mu_s} = \frac{(3.00 \text{ kg})(9.80 \frac{\text{m}}{\text{s}^2}) \sin 35.0^\circ}{0.300}$$

$$= 56.2 \text{ N}$$

Plug into (1) gives:

$$F = 56.2 \text{ N} - (3.00 \text{ kg})(9.80 \frac{\text{m}}{\text{s}^2}) \cos 35.0^\circ = \boxed{32.1 \text{ N}}$$