

**Basic Rules of Boolean Algebra**

	<b>OR</b>	<b>AND</b>	<b>XOR</b>
<b>Combined w/0</b>	$A+0=A$	$A\cdot 0=0$	$A\oplus 0=A$
<b>Combined w/1</b>	$A+1=1$	$A\cdot 1=A$	$A\oplus 1=\bar{A}$
<b>Combined w/self</b>	$A+A=A$	$A\cdot A=A$	$A\oplus A=0$
<b>Combined w/inverse</b>	$A+\bar{A}=1$	$A\cdot\bar{A}=0$	$A\oplus\bar{A}=1$
<b>Other rules</b>	$A+A\cdot B=A$	$A+\bar{A}\cdot B=A+B$	$(A+B)\cdot(A+C)=A+B\cdot C$
<b>DeMorgan's Th.</b>	$\overline{A\cdot B}=\bar{A}+\bar{B}$		$\overline{A+B}=\bar{A}\cdot\bar{B}$

Prove each of the following theorems using the basic rules of boolean algebra shown above.

*Please show all intermediate steps.*

1.  $A + \overline{A \cdot B} = 1$

2.  $D + D \cdot \bar{B} + D \cdot \bar{C} = D$

3.  $A \cdot (C + \bar{A}) + \bar{A} + \bar{C} = 1$