Points missed:	Student's Name:				
Total score:/100 points					
East Tennessee State Uni CSG	versity – Department of CI 2710 (Tarnoff) – Discr TEST 3 for Fall Semes	rete Structures	matic	on Sciences	
	Read this before sta	rting!			
 This test is closed book and close. You may NOT use a calculator. All answers must have a box draw Failure to do so might result in a second of the second of t	awn around them. This is no credit for answer. It is a page in this test, intermined. It is disciplinary action. Any act, the changing of falsifying of daid in tests, examinations, on the soft the offense and may in	dicate that you have 5.7 of the East Tenn et of dishonesty in acade any academic document other assigned school v clude, but are not limited	done essee emic v ts or r vork. d to: a	e so in case the need e State University vork constitutes academic naterials, cheating, and Penalties for academic n grade of 'F' on the work	
	QUESTIONS BEGIN	HERE!			
For problems 1 though 3, let $A = \{1\}$ relations R from A to B in these pro-		-	ethe	r the each of the	
1. $R = \{(1, a), (2, b), (1, b), (5, a), (2, b), (3, b), (4, b), (5, a), (5, a), (5, a), (6, b), (6, a), (6, b), (6, a), (6, a), (6, b), (6, a), (6, $	(4,b)	Function		Not a function	
2. $R = \{(1, a), (2, b), (3, b)\}$		Function		Not a function	
3. $R = \{(5, b), (4, c), (3, a), (2, a),$	(1,b)	Function		Not a function	
For problems 4 through 6, determin = b, then what is the set of all value	<u> </u>	•		n other words, if $f(a)$	
4. $a \in A = \text{Real numbers}; f(a) = a$	2 Ra	Range of <i>f</i> (a) =			
5. $a \in A = Positive integers; f(a) =$	= a (mod 5) Ra	Range of <i>f</i> (a) =			
6. $a \in A = \text{Integers}; f(a) = 2 \cdot a + 1$	Ra	Range of <i>f</i> (a) =			
For problems 7 though 9, let the until the output of the given characteristic		-	en the	e subset A, determine	
7. $A = \{t, h, o, m, a, s\}$	$f_{A}($	$f_{A}(b) = \underline{\hspace{1cm}}$			
8. $A = \{a, e, i, o, u\}$	$f_{A}($	y) =			
9. $A = \{b, o, r, i, n, g\}$	$f_{\rm A}($	b) =			

For problems 10 through 12, let f be the mod-20 function. Compute the output for each of the problems. (2 points each)

13. Assume that a hashing function *h* is used to store customer records to one of *n* linked lists. If each customer is assigned a unique 6-digit account number and the hashing function h is the mod 101 function, then how many linked lists will be needed? (2 points)

c.)
$$2^6 - 1$$

 \square **R** is a rooted tree

 \square **R** is a rooted tree

$$g.) 10^6$$

h.)
$$10^6 - 1$$

 \square **R** is not a rooted tree

 \square **R** is not a rooted tree

For problems 14 through 17, each relation \mathbf{R} is defined on the set \mathbf{A} . In each case, determine if \mathbf{R} is a **rooted** tree, and if it is, what is the root? If there is no root, leave that space blank. (3 points each)

14.
$$A = \{a, b, c, d, e\}$$

 $R = \{(a, b), (a, c), (e, d), (d, a)\}$

15.
$$\mathbf{A} = \{q, r, s, t, u, v\}$$

 $\mathbf{R} = \{(t, r), (u, s), (u, v), (s, q), (q, r), (s, t)\}$

16.
$$\mathbf{A} = \{1, 2, 3, 4, 5\}$$

 $\mathbf{R} = \{(1, 3), (1, 2), (5, 3), (2, 4)\}$

17.
$$\mathbf{A} = \{1, 2, 3, 4, 5\}$$

 $\mathbf{R} = \{(4, 5), (1, 2), (3, 4), (2, 3)\}$

If **R** is a rooted tree, the root is:

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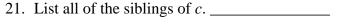
If **R** is a rooted tree, the root is:

For problems 18 through 24, use the rooted tree T shown in the figure to the right. (2 points each)

18. What is the height of *T*?

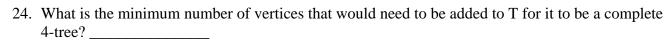
19. *T* is an *n*-tree. What is the value of *n*?

20. List all of the leaves of *T*.

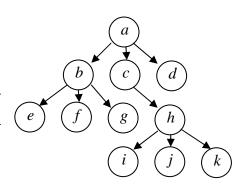


22. List all of the offspring of *c*.

23. List all of the descendants of *c*.



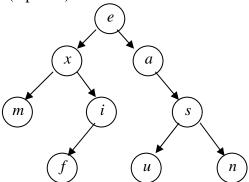
25. Construct the tree of the algebraic expression $((3-b)+(4\times c))-5$. (5 points)



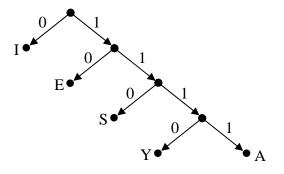
26. The following is the doubling linked list representation of a binary positional labeled tree. Construct the digraph of this tree with each vertex labeled as indicated. (6 points)

index	left	data	right
1	5		0
2	0	A	0
3	9	Н	7
4 5 6	0	I	2
5	3	T	4
6	0	Y	0
7	8	Е	6
8	0	S	0
9	0	S	0

27. Fill in the LEFT and RIGHT arrays in the table to the left for the tree shown below. Note that I want you to put the root vertex starting at index 7. (6 points)



- index left data right 1 2 m3 i 4 х 5 6 S 7 8 u9 n10 a
- 28. Use the Huffman code tree shown to the right to find the string of 0's and 1's that represents the word **SAY**. (4 points)



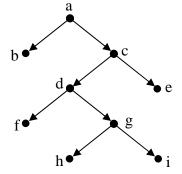
- 29. Use the Huffman code tree shown to the right to decode the message **01101011111101110**. (4 points)
- 30. The expression shown below is written in Polish (prefix) notation. Evaluate it to the final integer result. Note that all of the numbers are single digit integers. (3 points)

$$+-32\times6-42$$

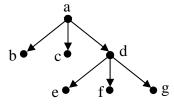
31. The expression shown below is written in reverse Polish (postfix) notation. Evaluate it to the final integer result. Note that all of the numbers are single digit integers. (3 points)

$$87 - 363 \div + \times$$

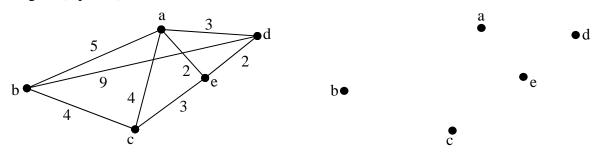
- 32. True or False: Parentheses are not needed in order to successfully evaluate expressions derived in any of the following notations: Polish (prefix), inorder (infix), or reverse-Polish (postfix). (2 points)
- 33. List the vertices in the order that they are visited in a preorder search of the tree shown to the right. (3 points)



- 34. List the vertices in the order that they are visited in an inorder search of the same tree from problem 33. (3 points)
- 35. In the space to the right, convert the tree shown below to a binary positional tree. (4 points)



36. Use any method you wish to determine the minimal spanning tree for the connected graph shown below and to the left. Draw the connections of the minimal spanning tree using the vertices shown to the right. (5 points)



- 37. True or False: There is more than one possible minimal spanning tree for the graph in problem 35. (2 points)
- 38. Make sure your name is on the front page. (1 point)