

Exercise A.1.95 Simplify  $\sqrt{(-4)^2}$ .

Solution

We work inside the square root first (because of the parentheses).

We have

$$\sqrt{(-4)^2} = \sqrt{(-4)(-4)} = \sqrt{16} = 4.$$

$$\text{So } \boxed{\sqrt{(-4)^2} = 4.}$$

Also, as we observed in Note A.1.E,

$$\sqrt{a^2} = |a| \text{ for any real number } a.$$

Applying this, we also get

$$\sqrt{(-4)^2} = |-4| = 4, \text{ as above. } \square$$