

# Calculus 1, Chapter 4 “Applications of Derivatives” Study Guide

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The following is a *brief* list of topics covered in Chapter 4 of *Thomas’ Calculus*.

**4.1 Extreme Values of Functions on Closed Intervals.** Absolute minimum and maximum, extreme values, Extreme-Value Theorem for Continuous Functions (Theorem 4.1), local maximum and minimum (relative extrema), Local Extreme Values (Theorem 4.2), critical point, finding extrema of continuous function on a closed and bounded interval.

**4.2 Mean Value Theorem.** Rolle’s Theorem (Theorem 4.3), Mean Value Theorem (Theorem 4.4), Functions with Zero Derivatives are Constant Functions (Corollary 4.1), Functions with the Same Derivative Differ by a Constant (Corollary 4.2), position/velocity/acceleration, Algebraic Properties of Natural Logarithms (Theorem 1.6.1/Theorem 4.2.A), Properties of Natural Exponentials (Theorem 4.2.B).

**4.3 Monotone Functions and the First Derivative Test.** increasing/decreasing function on an interval, monotonic function, First Derivative Test for Increasing and Decreasing (Corollary 4.3), First Derivative Test for Local Extrema (Theorem 4.3.A), sign tests of  $f'$ .

**4.4 Concavity and Curve Sketching.** Increasing/decreasing  $y'$ , concave up and concave down functions on open intervals, convex function, Second Derivative Test for Concavity (Theorem 4.4.A), concavity emojis, point of inflection, sign tests of  $f''$ , Second Derivative Test for Local Extrema (Theorem 4.5), “Procedure for Graphing  $y = f(x)$ ” (seven steps).

**4.5 Indeterminate Forms and L’Hôpital’s Rule**  $0/0$  and  $\infty/\infty$  indeterminate forms of limits, L’Hôpital’s Rule (Theorem 4.6), L’Hôpital’s Rule for  $\infty/\infty$  Indeterminate Forms (Theorem 4.5.A),  $\infty - \infty$  indeterminate form,  $0 \cdot \infty$  indeterminate form,  $1^\infty$  indeterminate form,  $0^0$  indeterminate form,  $\infty^0$  indeterminate form, limits and exponentials (Theorem 4.5.B), Cauchy’s Mean Value Theorem (Theorem 4.7), proof of L’Hôpital’s Rule.

**4.6 Applied Optimization Problems.** Solving Applied Optimization Problems (the 5 steps), cost/revenue/profit functions, marginal revenue, marginal cost, marginal profit, average cost function.

**4.7 Newton's Method.** The iterative procedure for Newton's Method, problems with Newton's Method (see Figures 4.53 and 4.54).

**4.8 Antiderivatives.** Antiderivative, indefinite integral, integral sign, variable of integration, the form of an indefinite integral and the “ $+C$ ” notation (see Theorem 4.8), differential equation, initial value problem, antiderivative formulas (Tables 4.2 and 4.2.A), Constant Multiple Rule and Sum or Difference Rule, general solution of a differential equation, initial conditions, and solution to an initial value problem.