

# Theory of Matrices, MATH 5090, Summer 2018

## Homework 9, Section 3.8

Due Friday, July 6 at 1:00

**Write in complete sentences!!!** *Explain* what you are doing and convince me that you understand what you are doing and why. Justify all steps by quoting relevant results from the textbook or hypotheses.

**3.16.** Prove Theorem 3.8.2(5): Let  $A$  be an  $n \times n$  real matrix with eigenpair  $c$  and  $v$ . If  $A$  is diagonal or triangular with diagonal entries  $a_{ii}$ , then the eigenvalues of  $A$  are  $a_{ii}$ . For  $A$  diagonal, the corresponding eigenvectors are  $e_i$  (the  $i$ th unit vector in  $\mathbb{R}^n$ ).

**3.18.** Prove Theorem 3.8.7(5): Let  $A$  be a real square matrix and  $(c, v)$  an eigenpair (possibly complex) for  $A$ . Prove that  $c$  is real if  $A$  is symmetric.

**3.8.B.** Let  $A$  be an  $n \times n$  (not necessarily symmetric) matrix. Let  $w$  be a left eigenvector for eigenvalue  $c$  and let  $v$  be a right eigenvector for eigenvalue  $c$ , where  $w^T v = 1$ . Prove that for  $k \in \mathbb{N}$ ,  $(A - cvw^T)^k = A^k - c^k vw^T$ .