

# Chapter 8. Symmetries of Knots

## Study Guide

The following is a brief list of topics covered in Chapter 8 of Charles Livingston's *Knot Theory*, The Carus Mathematical monographs, Volume 24 (MAA, 1993). This list is not meant to be comprehensive, but only gives a list of several important topics. You should also carefully study the proofs given in class and the homework problems.

### 8.1. Amphicheiral and Reversible Knots.

Reversible knot, positive/negative amphicheiral knot, strongly reversible knot, strongly positive/negative amphicheiral knot.

### 8.2. Periodic Knots.

Periodic knot of period  $q$ , quotient knot, covering link, linking number  $\lambda$ , the number of complements in  $L$  is the greatest common divisor of the linking number  $\lambda$  and  $q$  (Theorem 8.2.1).

### 8.3. The Murasugi Conditions.

The Murasugi Conditions (Theorem 8.3.2), irreducible polynomials over a field, applications of the Murasugi Conditions, the total degree and the mod  $p$  total degree of a polynomial.

### 8.4. Periodic Seifert Surfaces and Edmonds' Theorem.

Equivariant Seifert surface, a period  $q$  knot has a period  $q$  equivariant Seifert surface (Theorem 8.4.3), Riemann-Hurwitz Formula, relationship between the linking number  $\lambda$  and the number  $\Lambda$  of points of intersection of the Seifert surface with the  $z$ -axis (Theorem 8.4.5), Edmond's Conditions (Corollary 8.4.6).

### 8.5. Applications of the Murasugi and Edmonds Conditions.

Three corollaries following from the Murasugi and Edmonds Conditions (Corollaries 8.5.7, 8.5.8, and 8.5.9) and their applications.

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