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Some generalizations of the Eneström-Kakeya theorem.

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The authors give some generalizations of the Eneström theorem, which states that all the zeros of a polynomial, with positive real coefficients a_ν , lie in the annulus $\alpha \leq |z| \leq \beta$ when $\alpha = \min_{0 \leq \nu \leq n} \{a_\nu/a_{\nu+1}\}$ and $\beta = \max_{0 \leq \nu \leq n} \{a_\nu/a_{\nu+1}\}$. They prove Theorem 1, which states that all of the zeros of the polynomial $\sum_{\nu=0}^n (\alpha_\nu + i\beta_\nu)z^\nu$ lie in the annulus $R_1 \leq |z| \leq R_2$, where for some k and positive t , $\alpha_0 \leq t\alpha_1 \leq t^2\alpha_2 \leq \cdots \leq t^k\alpha_k \geq t^{k+1}\alpha_{k+1} \geq t^{k+2}\alpha_{k+2} \geq \cdots \geq t^n\alpha_n$ and the expressions for R_1 and R_2 involve α_ν , β_ν , k and t . From this theorem the authors derive two corollaries and two more theorems. In their example, they show that all the zeros of $1 + 10z + 20z^2 + 40z^3 + 80z^4 + 50z^5$ lie in $0.499 \leq |z| \leq 0.840$. *M. K. Jain*

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