While not a substitute for the valuable technique of logarithmic differentiation (the rule is a good exercise in it), it allows students to see the harmony in the various rules. Its similarity to the product rule, "take the derivative of f holding g constant plus the derivative of g holding f constant," adds to its appeal for students.

See FFF 47 in CMJ 22 (1991) 404.

## A Useful Notation for Rules of Differentiation

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The freshman calculus instructor is often faced with the task of deciphering the freshman calculus student's versions of the product rule, quotient rule and chain rule. Even when correctly computed, it can be difficult to follow the student's steps, especially when the differentiated function involves several trigonometric functions. I propose a notational convention to deal with this problem.

Several popular calculus books (e.g. Swokowski, Larson et al., etc.) represent the differential operator as  $D[\cdot]$  or  $d/dx[\cdot]$ . With this as motivation, I have used the following notation quite successfully in the classroom. Whenever a function is differentiated using the product rule, quotient rule, or chain rule, put the differentiated parts in square brackets. This means that the product rule would be written as

$$D[(f)(g)] = [f'](g) + (f)[g'].$$

In fact, if the instructor introduces the convention of "always differentiate f (the first function in the product) first," then the product rule can be presented pictorially as

$$D[(\ )(\ )] = [\ ](\ ) + (\ )[\ ].$$

This reduces exercises involving the product rule to nothing more than fill-in-theblank problems.

Similarly, the quotient rule can be represented as

$$D\left[\frac{(\ )}{(\ )}\right] = \frac{[\ ](\ ) - (\ )[\ ]}{(\ )^2}.$$

The habit of "differentiating f first" developed in the product rule, must be carried over to the quotient rule.

The chain rule is a bit harder to "draw"; however the special case known as the power rule can be illustrated in this manner:

$$D[()^n] = n()^{n-1}[].$$

My experience has shown that, not only is the students' work easier to follow, but the material is easier to present clearly. Students have reacted quite positively to this notation. In fact, when encouraged to adopt the notation, but not required to, I have found that practically all students choose to use the notation. This has been the case even when the notation was introduced some time after the rules of differentiation, i.e., Calculus 2 and Calculus 3 students quickly "pick up the habit."

An example illustrates the utility of this method. Suppose

$$f(x) = \frac{\sec x \tan x}{\left(x^2 + 1\right)^6}.$$

With the notation,

$$f'(x) = \frac{\left[\left[\sec x \tan x\right](\tan x) + \left(\sec x\right)\left[\sec^2 x\right]\right](x^2 + 1)^6 - \left(\sec x \tan x\right)\left[6(x^2 + 1)^5[2x]\right]}{\left(x^2 + 1\right)^{12}}$$

Although a formidable derivative, it can be viewed as nothing more than a large fill-in-the-blank problem.

With the square brackets, it is much easier to follow the students' steps and, if applicable, to give partial credit. In fact, give the above problem on your next calculus test. I think, in the absence of the square brackets, you will find it quite a task simply to determine if the students' responses are partially correct!

Mathematics the Mother of Writing 2:19:10 - 1155 (19:28-917) [771/71] 11 27 39:11 tants, beginning perhaps 10,000 years ago in the Fertile Crescent as a kept track of their sheep; cows, grain and wine by counting bean-like pieces of and mathematics; according to archeologist. Denise Schmandt-Bessel the University of Texas at Austin Sometime around 8000 BC; a particularly bright individual made Schmandt-Besserat called a "conceptual leap". That person recognize That accountants routh make small cravitokens whose is been Archeologists have now found 15 main voes of waround 3300 BC rusomeone invented envelopes, called "bullac A CHARLES THE HEALTH AND A CHARLES HOLD SO THE CONTROL OF THE CONT discerned without breaking them open www. with was with a in it of overcome this problem haccountants began pressing the toke the clay before closing the envelope; and hardening it has a factor of This simple change, from tokens to their negative impression face of a clay tablet, can now be recognized as the invention of writing,