

## General Physics II Lab (PHYS-2021)

### Experiment WAVE-1: Vibrating Strings

#### 1 Equipment

##### INCLUDED:

1	String Vibrator	WA-9857
1	Physics String	SE-8050
1	Force Sensor	PS-2104
1	C-clamp (small)(only need one)	SE-7286
1	Patch Cords (set of 5)	SE-9750
1	Tape Measure	SE-8712A
1	850 Universal Interface	UI-5000
1	PASCO Capstone	UI-5400

#### 2 Introduction

The general appearance of waves can be shown by means of standing waves in a string. This type of wave is very important because most of the vibrations of extended bodies, such as the prongs of a tuning fork or the strings of a piano, are standing waves. The purpose of this experiment is to examine how the tension required to produce a standing wave in a vibrating string of fixed length and mass density is affected by the wavelength and the frequency of the wave. This is a hands-on experiment where the student gets to feel the force required to increase the number of vibrating segments. This experiment requires a formal Lab Report as described in the “Lab Report Format” document.

#### 3 General Theory

Standing waves (stationary waves) are produced by the addition of two traveling waves, both of which have the same wavelength and speed, but travel in opposite directions through the same medium. Figure 1 shows such a system, where a mechanical vibrator produces a wave on a string which moves to the right and reflection from a fixed end produces a left moving wave. Where the two waves are always  $180^\circ$  out of phase, very little motion occurs (none if the amplitudes are the same). Such places are called nodes (see Figure 1). Where the two waves are in phase, the motion is maximum. These positions are called anti-nodes. Figure 2 shows a representation of a standing wave. This representation shows the two extreme positions of the string. This matches well what the eye or camera sees since the string speed is minimum at the extremes. However, don't forget that the string goes through all of the positions in between the extremes as shown by the blur in Figure 1. Note that as shown in Figure 2, the node-to-node distance is one-half of the wavelength. The necessary conditions for the production of standing waves on a stretched string fixed at both ends is the length of the string be equal to an integer

number of half wavelengths so that there can be a node at each fixed end. For this experiment, one fixed end is where the string attaches to the force sensor and the other is where the string attaches to the mechanical vibrator. The end attached to the force sensor is a true node, but the end attached to the metal wand on the vibrator is not exactly a node since the wand vibrates up a little. Close examination (see Figure 3) shows that the true node would be a little to the left of the knot so the effective string length will be a bit longer than we measure. However, the difference does not appear to be more than a few millimeters, so is only a fraction of a percent.

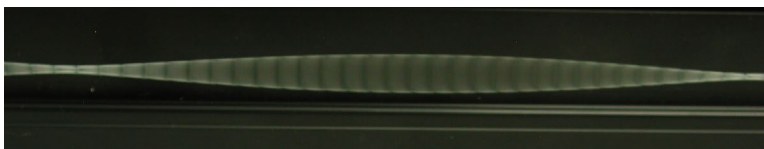


Figure 1: Standing Wave Photo

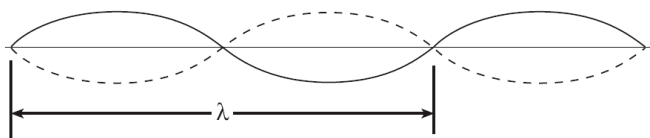


Figure 2: Standing Wave Representation

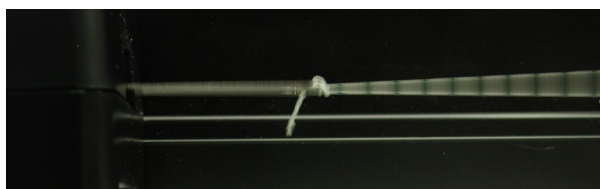


Figure 3: Vibrator ~ Node

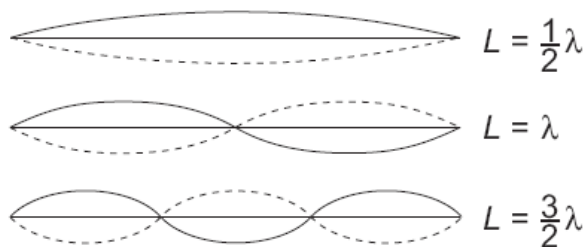


Figure 4: Modes of Vibration

#### 4 Theory: Standing Waves in Strings

A stretched string has many natural modes of vibration (three examples are shown in Figure 4 above). If the string is fixed at both ends then there must be a node at each end. It may vibrate as

a single segment, in which case the length ( $L$ ) of the string is equal to  $1/2$  the wavelength ( $\lambda$ ) of the wave. It may also vibrate in two segments with a node at each end and one node in the middle; then the wavelength is equal to the length of the string. It may also vibrate with a larger integer number of segments. In every case, the length of the string equals some integer number of half wavelengths. If you drive a stretched string at an arbitrary frequency, you will probably not see any particular mode; many modes will be mixed together. But, if the tension and the string's length are correctly adjusted to the frequency of the driving vibrator, one vibrational mode will occur at a much greater amplitude than the other modes.

For any wave with wavelength  $\lambda$  and frequency  $f$ , the speed,  $v$ , is

$$v = \lambda f \quad \text{Eq. (1)}$$

The speed of a wave on a string is also related to the tension in the string,  $F$ , and the linear density (=mass/length),  $\mu$ , by

$$v^2 = F / \mu = \lambda^2 f^2 \quad \text{Eq. (2)}$$

$L$  is the length of the string and  $n$  is the number of segments. (Note that  $n$  is *not* the number of nodes). Since a segment is  $1/2$  wavelength then

$$\lambda = 2L / n \quad \text{where } n = 1, 2, 3, \dots \quad \text{Eq. (3)}$$

Solving Equation 2 for the tension yields:

$$F = \mu \lambda^2 f^2 \quad \text{Eq. (4)}$$

In the first part of the experiment, we will hold  $\lambda$  constant by always choosing a two-segment pattern so that  $\lambda = L$  since  $n = 2$  and vary the frequency while measuring the tension at which a two-segment standing wave appears. By plotting  $F$  versus  $f^2$ , we should see a straight line with a slope of  $\mu\lambda^2$ .

In the second part, we hold the frequency constant and vary the tension Figure 4 to get standing waves with different numbers of segments, so different values of  $\lambda$ . Plotting  $F$  versus  $\lambda^2$  should give a straight line with slope  $\mu f^2$ .

## 5 String Mass Density

Each lab group will use a piece of PASCO Physics String about one meter long. However, the mass of 1 m of string is about  $1/4$  g which is too small for most scales to measure with much precision. Fortunately, the Physics String is very uniform (varies by less than 1%) and not very stretchy, so we can measure the mass of a long piece and then cut it into 1 m segments that will have nearly the same mass density as average mass density of the long piece.

1. Determine the number of lab groups. Cut a piece of string that is long enough to provide each group with 1 m of string. That is, if there are five lab groups, cut a piece of string that is about 5 m long (or longer).
2. Use the tape measure to determine the length of the string to a precision of +/- 1 cm. Enter this value in the “Length of String” column of the String Mass Density table.
3. Use the best available scale to determine the mass of the string. Ideally, use a digital scale with a precision of 0.01 g. To achieve this precision: 1) zero the scale; if it doesn't read exactly zero, record the value including sign, 2) add the string and record the string mass [don't forget to correct for the zero reading if it wasn't zero], 3) remove the string and verify that the zero reading hasn't changed, 4) if the zero value did change, repeat until you get consistent values. If you are using a single pan balance, the precision is 0.1 g. To achieve this precision, either zero the scale carefully or note where the equilibrium position is with nothing in the pan and use that position to achieve balance. Enter the value in the “String mass” column of the String Mass Density table. Note that the program then calculates the “mass density” = “String mass”/“Length of String”.
4. The uncertainty in the “mass density” arises from the measurement of the “String mass”. If the “String mass” was 2.0 g measured with a single pan balance, the precision is 0.1 g and the uncertainty would be  $(0.1 \text{ g}/2.0 \text{ g}) \times 100 = 5\%$ . Similarly, using a good digital scale, the numbers might be 2.00 g +/- 0.01 g and the uncertainty would be  $(0.01 \text{ g}/2.00 \text{ g}) \times 100 = 0.5 \%$ . However, you should not claim an uncertainty less than 1% since the string can vary by 1% in its mass density. Enter your estimate for the uncertainty in column 4 of the String Mass Density table.
5. Cut a piece of string about 1 m long for each lab group.

## 6 Setup

1. Setup as shown in Figure 5. Clamp the String Vibrator firmly to the table. Attach two banana cables from Output 1 on the 850 Universal Interface to the Inputs on the String Vibrator. Polarity does not matter.
2. Attach the Force Sensor to any of the *PasPort* inputs on the 850 Universal Interface.
3. Tie the 1 m string to the hook on the Force Sensor and to the vibrating blade on the String Vibrator.
4. The oscillation of the string is all in a vertical plane. It is nice to provide a dark backdrop so the student can see the pattern better. One nice solution is to use a PASCO Optics Bench (OS-8541 or OS-8508) on edge as shown in Figure 6.
5. The Standard Setup has the advantage of giving the student some direct tactile experience of how tension is related to wavelength. However, the accuracy can be improved with the Alternate Setup in Figure 6. Here the Force Sensor is attached to a steel rod (ME-8736) using the thumbscrew of the Force Sensor. The steel rod is clamped in the Large Rod Base (ME-8735) which can be moved to vary the tension. This makes it possible to control the tension and find the maximum standing wave more precisely.



Figure 5: Standard Setup



Figure 6: Alternate Setup

## 7 Constant Wavelength Procedure: (sensors 20 Hz)

1. Move the Force Sensor so the string is under tension and determine the length of the string between the knot attached to the blade on the String Vibrator and the knot attached to the hook on the Force Sensor. We will adjust for two segments (as in Figure 5) for each case, so the knot to knot distance will be the wavelength. Record your value in the Wavelength table to the right.
2. Click on the Signal Generator at the left of the screen. Open Output 1 and set for a Sine Waveform at an Amplitude of 5 V and a frequency of 60 Hz. You may vary the Amplitude during the experiment. Increasing the Amplitude will increase the size of the standing wave. **DO NOT exceed 10 V!** If the String Vibrator begins to clatter, it is being overdriven and you should decrease the Amplitude.
3. Click On to turn the String Vibrator on.
4. Adjust the tension in the string to get the string vibrating in two segments (as in Figure 5) and to maximize the amplitude of the standing wave. It is easiest to start with the tension too high and slowly decrease it.
5. When you have the maximum standing wave, click RECORD and collect data for about 10 seconds. Click STOP.
6. The force shown in the String Tension box is the average value over the 10 seconds. Ignore the minus sign. Record this value in the “Tension” column of the Constant Wavelength table in the 60 Hz row.
7. Repeat for frequencies of 85 Hz, 104 Hz, 120 Hz, 134 Hz, and 147 Hz.

Question: why this rather strange looking choice of frequencies? Hint: see the Constant Wavelength graph on the next page.

## 8 Constant Wavelength Analysis:

1. Based on Equation 4 from Standing Wave Theory, what should be the slope and y-axis intercept of the Tension vs frequency<sup>2</sup> plot? Include an estimate of the uncertainty in the slope. The uncertainty here is due to the uncertainty in the mass density, so the % uncertainty in the calculated slope is the same as the % uncertainty in the mass density from the String Mass Density table under the String Mass tab.
2. Click on the Scale to Fit icon from the graph toolbar.
3. Click on the black triangle by the Curve Fit icon on the graph toolbar and select Linear.
4. How well do the experimental slope and intercept from step 2 agree with the value you calculated for slope and intercept in step 1? Discuss briefly. What does this show?

## 9 Constant Frequency Procedure: (sensors 20 Hz)

1. Move the Force Sensor so the string is under tension and determine the length of the string between the knot attached to the blade on the String Vibrator and the knot attached to the hook on the Force Sensor. If the setup is the same as you used in the Constant  $\lambda$  Procedure, just use the value you measured there which is given in the Wavelength table under the Constant  $\lambda$  Procedure tab. Enter this length in the “String Length” column of the Constant Frequency table in each of the five rows (same value in each row).
2. Click on the Signal Generator at the left of the screen. Open Output 1 and set for a Sine Waveform at an Amplitude of 5 V and a frequency of 150 Hz. You may vary the Amplitude during the experiment. Increasing the Amplitude will increase the size of the standing wave. **Do Not exceed 10 V!** If the String Vibrator begins to clatter, it is being overdriven and you should decrease the Amplitude.
3. Click On to turn the String Vibrator on.
4. Adjust the tension in the string to get the string vibrating in one segment (nodes only at the ends) and to maximize the amplitude of the standing wave. It is easiest to start with the tension too high and slowly decrease it. **Note:** *You may have a lot of trouble getting the fundamental wavelength in addition to the higher  $n$  waves mentioned below. If you have this difficulty, just do the higher harmonics in #7 below (e.g.,  $n = 2, 3, 4, 5, 6$ ) and not bother with  $n = 1$ , the fundamental wavelength.* OPTIONAL NOTE: The issue that arises in measuring the first harmonic wave is that there is not enough friction between the iron ring stand and the table top to keep the string from sliding back. Should you wish to measure the first harmonic wave, one can increase the tension in the string by using your hand to keep the ring stand still. Just keep your hand steady to keep the force stable.
5. When you have the maximum standing wave, click RECORD and collect data for about 10 seconds. Click STOP.
6. The force shown in the Tension Force box is the average value over the 10 seconds. Ignore the minus sign. Record this value in the “Tension Force” column of the Constant Frequency table in the first row.
7. Repeat for standing wave patterns with 2, 3, 4, and 5 segments.

## 10 Constant Frequency Analysis

1. Based on Equation 4 from Standing Wave Theory, what should be the slope and y-axis intercept of the Tension vs wavelength<sup>2</sup> plot? Include an estimate of the uncertainty in the slope. The uncertainty here is due to the uncertainty in the mass density, so the % uncertainty in the calculated slope is the same as the % uncertainty in the mass density from the String Mass Density table under the String Mass tab.
2. Click on the Scale to Fit icon from the graph toolbar.
3. Click on the black triangle by the Curve Fit icon on the graph toolbar and select Linear.
4. How well do the experimental slope and intercept from step 2 agree with the value you calculated for slope and intercept in step1? Discuss briefly. What does this show?